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Mostafa Sulaiman, Eric Climent, Anthony Wachs, Abdelkader Hammouti. Numerical simulations and modelling of mass transfer through random assemblies of catalyst particles: from dilute to dense reactive particulate regime. Chemical Engineering Science, 2020, 223, pp.115659. 10.1016/j.ces.2020.115659. hal-02940301

HAL Id: hal-02940301 https://ifp.hal.science/hal-02940301

Submitted on 30 Apr 2021

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https://doi.org/10.1016/j.ces.2020.115659

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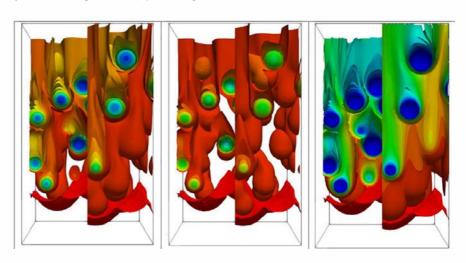
Sulaiman, Mostafa and Climent, Éric and Wachs, Anthony and Hammouti, Abdelkader *Numerical simulations and modelling of mass transfer through random assemblies of catalyst particles: from dilute to dense reactive particulate regime.* (2020) Chemical Engineering Science, 223. 115659. ISSN 0009-2509

Numerical simulations and modelling of mass transfer through random assemblies of catalyst particles: From dilute to dense reactive particulate regime

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G R A P H I C A L A B S T R A C T



ABSTRACT

We study mass transfer through random assemblies of fixed spherical catalyst particles experiencing an external convective diffusive fluid stream. Chemical species are transported through the array and are diffused from fluid to solid phase through particles surface. An internal first order irreversible chemical reaction takes place within the porous catalyst particles. We address the determination of mass transfer coefficient by performing direct numerical simulations with fully internal external coupling using con centration and flux continuity boundary conditions at the solid fluid interface. We derive a theoretical prediction of the profiles of cup mixing concentration, average of mean surface and average of mean vol ume concentration of the particles along the height of the domain. The model for the dimensionless mass transfer coefficient ('reactive' Sherwood number) is accounting for the five dimensionless parameters that control the physics of the system: the Reynolds number Re, the Schmidt number Sc, the Damköhler number Da, the internal to external diffusion coefficient ratio γ and the solid volume fraction α_s . We use a coupled Sharp Interface/ Discrete Lagrange Multiplier Fictitious Domain Method (SIM DLM/FD), thoroughly validated in our previous study (Sulaiman et al., 2019) to test the accuracy of the model

Keywords:
Porous catalyst particles
Chemical reaction
Mass transfer
Direct numerical simulations
Sherwood number

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1. Introduction

Chemical reactors composed of solid particles dispersed in a fluid phase are commonly operated in many industrial facilities. In petrochemical processes, catalytic fixed bed reactors (Wehinger et al., 2015) and catalytic fluidized bed reactors (Gao et al., 2008) are widely operated in refineries for cracking long chain hydrocarbons into lighter products. Biomass catalytic co pyrolysis processes (Zhang et al., 2018), biomass gasification (Bridgwater, 1995; Turn et al., 1998) and biomass complete com bustion (Baxter, 1993) are processes involving multiphase flows with chemical reactions in particles. In such systems, many trans port phenomena take place, such as heat, mass, and momentum transfer. The performance prediction, design, and optimization of these reactors necessitate a better comprehension of the coupling among the various occurring physical and chemical phenomena taking place in there.

Particle Resolved Direct Numerical Simulations (PR DNS or PRS) that fully resolve local interactions between the two phases is an emerging approach to understand the coupling between transport phenomena and chemical reactions. Indeed, high perfor mance computing with increasing CPU efficiency has encouraged scientists to develop numerical methods to solve momentum and mass balance equations on grids finer than the particle size. PRS is able, so far, to simulate particulate flow systems consisting of thousands of particles and provide reliable information about local interactions at the particle scale (Sun et al., 2016). However, DNS is unable to simulate industrial scale systems that contain billions of particles. The local interactions resolved by DNS at the particle scale can be modeled by correlations or closure laws, such as a drag coefficient correlation for momentum transfer (Deen et al., 2014), a Nusselt number correlation for heat transfer and a Sherwood num ber correlation for mass transfer. In fluidized beds or turbulent flows seeded with particles, the solid volume fraction varies over a wide range from dilute to dense regions due to preferential accu mulation and the formation of clusters. These closure laws can be used in a multi scale analysis (van der Hoef et al., 2004) to enhance the accuracy of numerical methods such as CFD DEM, that are able to simulate systems with large number of particles but do not resolve the flow and transfers below the particle scale.

Many PRS methods are available in literature to simulate partic ulate flow problems. The methods with a fixed Cartesian mesh have the advantage of very good scalability on supercomputers. Their disadvantage lies in the difficulty of imposing accurately the correct boundary conditions on the surface of each particle. The Immersed Boundary Method (IBM) (Uhlmann, 2005), is a fixed mesh computational method, that imposes boundary conditions at the particle surface by means of Lagrangian markers. Both the smooth version of (Uhlmann, 2005) and a high order ghost cell version have been applied by Xia et al. (2014) to study convective heat/mass transfer for a single particle. IBM was also used to eval uate the heat transfer Nusselt number in dense particulate flow systems by Deen et al. (2014) and Sun et al. (2015). More recently, Lu et al. (2018) employed an IBM to study mass transfer with a first order irreversible surface chemical reaction. (Derksen, 2014) cou pled IBM with the Lattice Boltzmann Method (LBM) to study mass transfer through fixed and fluidized beds of particles. (Bohn et al., 2012) studied gas solid diffusion reaction within a single particle. The Distributed Lagrange Multiplier/ Fictitious Domain Method

(DLM/FD) is an alternative approach. Firstly introduced by Glowinski et al. (2001), and it combines the particle and fluid bal ance equations into a general weak formulation on a fixed Carte sian mesh. The DLM/FD method has been used to simulate heat/mass transfer by Yu et al. (2006),Dan and Wachs (2010) and Wachs (2011).

In addition, the Sharp Interface Method (SIM), or as alterna tively referred to, the Ghost Fluid Method (GFM), is a fixed mesh computational method that accurately enforces boundary conditions with discontinuities along embedded interfaces (Shi et al., 2011). Jump conditions are incorporated into the discretization of the differential operators on a Cartesian grid in the vicinity of the interface. The SIM was firstly introduced by Fedkiw et al. (1999). Shao et al. (2012) combined the SIM with a fictitious domain method to simulate heat transfer inside and outside particles. More recently, Sulaiman et al. (2019b) coupled the SIM to a fictitious domain method to study mass transfer for three interacting aligned catalyst particles undergoing a first order irreversible chemical reaction.

In this work, we study the effect of a first order irreversible chemical reaction on mass transfer in a random assembly of fixed particles. The reaction takes place within the catalyst particles composing the assembly. The fluid enters the system with an imposed inlet concentration and transports chemical species through the particle array. For infinite reaction rate, the system is analogous to heat transfer problems (Sun et al., 2016; Deen et al., 2014; Tavassoli et al., 2013 and Gunn, 1978) for which tem perature is imposed at the particle surface. The analogy with heat transfer fails when the reaction rate is finite. According to the reac tion kinetics, one of the three following regimes can predominate. (i) When the reaction rate is very slow compared to diffusion, the surface concentration of the particles is equal to the bulk concen tration in the fluid and the regime is chemically controlled. (ii) When the reaction rate is infinitely fast compared to diffusion, the surface concentration approaches zero and the system is con trolled by mass transfer (diffusion limited), (iii) In between the two previous cases, the system is neither mass transfer controlled nor kinetics controlled, and the catalyst surface concentration is a priori unknown. In our previous work (Sulaiman et al., 2019a) and Sulaiman et al. (2019b), for a single particle and three interacting particles, respectively, we presented models for the 'reactive' Sher wood number that accounts for the effect of an internal chemical reaction and diffusion in the solid phase coupled to external con vection and diffusion in the fluid phase.

Our objective in the present work is to extend our model to account for the effect of the solid volume fraction on the reactive Sherwood number in the flow through a random array of fixed reactive particles. We do not consider the specific case of closely packed bed reactors but address more generally the effect of solid volume fraction on mass transfer as would be the case of solid par ticles suspended in a fluid flow. The paper is organized as follows. First, we introduce the balance equations and the numerical method is briefly described referencing former papers on bench marks and validations. We describe also the numerical setup for the simulation in a random assembly of particles. In the third sec tion, we present the theoretical modeling of mass transfer coupled to chemical reaction which has been extended in the present paper to account for the effect of solid volume fraction. Finally numerical simulation results are compared to the theoretical prediction and

conclusions are drawn on the range of validity and limitations of the present approach.

2. Balance equations and numerical setup

2.1. Governing equations

We solve the time dependent and incompressible flow of a Newtonian fluid around multiple fixed solid particles with mass transfer from the fluid to particles. Chemical reaction occurs within the solid catalytic porous particles without considering heat trans fer. Only diffusion is considered inside the particles because we assume permeability to be low. We define the full flow domain as Ω , the part of Ω occupied by the solid particles as P and the part of Ω occupied by the fluid as $\Omega \setminus P$. The problem is governed by the fluid mass conservation equation, fluid momentum balance and chemical species transport and reaction equations. The fluid den sity and viscosity are considered to be constant by assuming a sin gle solute under low concentration C in the fluid. Dimensional quantities are distinguished from dimensionless quantities by a '*' superscript. We denote u^* the fluid velocity, p^* the fluid pres sure, C_f^* the chemical species concentration in the fluid and C_s^* the chemical species concentration in the particles. The chemical species is undergoing a first order irreversible reaction in the solid particles. With appropriate initial conditions in Ω on $(\boldsymbol{u}^*, C_f^*, C_s^*)$ and boundary conditions on $\partial\Omega$, the boundary of Ω , on \boldsymbol{u}^* (and potentially on p^*), the set of conservation equations together with fluid/solid interface conditions is written as follows:

• in the fluid

$$\rho_{f}^{*} \left(\frac{\partial \mathbf{u}^{*}}{\partial t^{*}} + (\mathbf{u}^{*} \cdot \nabla) \mathbf{u}^{*} \right) \quad \eta^{*} \nabla^{2} \mathbf{u}^{*} + \nabla p^{*} \quad \mathbf{0}, \tag{1}$$

$$\nabla \cdot \mathbf{u}^{*} \quad 0, \tag{2}$$

$$\frac{\partial C_{f}^{*}}{\partial t^{*}} + \mathbf{u}^{*} \cdot \nabla C_{f}^{*} \quad \nabla \cdot \left(D_{f}^{*} \nabla C_{f}^{*} \right) \quad 0, \tag{3}$$

$$\nabla \cdot \mathbf{u}^* = 0,$$
 (2)

$$\frac{\partial C_f^*}{\partial t^*} + \boldsymbol{u}^* \cdot \nabla C_f^* \quad \nabla \cdot \left(D_f^* \nabla C_f^* \right) \quad 0, \tag{3}$$

where ρ_f^* denotes the fluid density, η^* the fluid viscosity and D_f^* the chemical species diffusion coefficient in the fluid.

• in the solid

$$\mathbf{u}^* = 0,$$
 (4)

$$\frac{\partial C_s^*}{\partial t^*} \quad \nabla \cdot \left(D_s^* \nabla C_s^* \right) \qquad k_s^* C_s^*, \tag{5}$$

where D_s^* denotes chemical species effective diffusion coeffi cient and k_s^* the effective first order reaction constant in the solid. The molecular diffusion and reaction constant of the kinetics are related to the internal micro structure of the por ous media (porosity, tortuosity and specific area for the cat alytic reaction). We thus assume that they can be approximated by a continuous model in which the effective dif fusion coefficient in solid phase is typically ten to hundred times lower than in fluid phase. Bruggeman's correlation states that tortuosity scales with porosity to the power 1/2 yielding in our cases a porosity of catalytic particles varying from 0.04 and 0.2. Therefore, the flow cannot penetrate within particles of very low permeability and the reactive solute only diffuses inside the catalytic porous particles.

at the fluid/solid interface ∂P

$$\mathbf{u}^* = \mathbf{0},$$
 (6)

$$C_s^* C_f^*, (7)$$

$$D_{s}^{*} \frac{\partial C_{s}^{*}}{\partial \mathbf{n}} \qquad D_{f}^{*} \frac{\partial C_{f}^{*}}{\partial \mathbf{n}}, \tag{8}$$

where n denotes the unit vector normal to the fluid/solid inter face. Balance equations are made dimensionless by introducing a characteristic length L_c^* , a characteristic velocity U_c^* and a charac teristic convective time T_c^* L_c^*/U_c^* . As solid particles are spheres, we choose L_c^* as particle diameter d_p^* . When the problem is not purely diffusive, an obvious choice for U_c^* is the far field inlet velocity U_{in}^* . Also, by normalizing the chemical species concen tration between 0 and 1 and introducing the chemical species diffusion coefficient ratio $\gamma = \frac{D_s^*}{D_s^*}$, conservation Eqs. (3) and (5) together with boundary conditions (7) and (8), i.e., continuity of chemical species concentration and continuity of chemical species normal flux density, can be recast into a single dimen sionless conservation equation for the chemical species C with appropriate continuity conditions at the fluid/solid interface on the chemical species concentration and on its normal flux. The set of dimensionless equations eventually reads as follows:

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla)\mathbf{u} \quad \frac{1}{Re} \nabla^2 \mathbf{u} + \nabla p \quad \mathbf{0} \quad \text{in} \quad \Omega \setminus P, \tag{9}$$

$$\nabla \cdot \mathbf{u} \quad 0 \quad \text{in} \quad \Omega \setminus P, \tag{10}$$

$$\mathbf{u} \quad \mathbf{0} \quad \text{in} \quad P \cup \partial P, \tag{11}$$

$$\nabla \cdot \boldsymbol{u} = 0 \quad \text{in} \quad \Omega \setminus P,$$
 (10)

$$\mathbf{u} \quad \mathbf{0} \quad \text{in} \quad P \cup \partial P, \tag{11}$$

$$\frac{\partial C}{\partial t} + \mathbf{u} \cdot \nabla C \quad \nabla \cdot \left(\frac{h(\gamma)}{Pe} \nabla C \right) + \frac{h(\gamma)g(\phi^2)}{Pe}$$

$$C \quad 0 \quad \text{in} \quad \Omega, [C]_{\partial P} \quad 0, \quad \left[h(\gamma) \frac{\partial C}{\partial \mathbf{n}} \right]_{\partial P} \quad 0, \tag{12}$$

where $[]_{\partial P}$ represents the jump condition across the fluid/solid interface. The dimensionless numbers introduced above are defined as follows:

- Reynolds number: $Re^{-\frac{\rho_{f}^{*}U_{c}^{*}L_{c}^{*}}{n^{*}}}$, characterizes the external flow
- Peclet number: $Pe = \frac{U_c^* L_c^*}{D_i^*}$, characterizes convective to diffusive external transport,
- Damköhler number: Da ϕ^2 $\frac{k_s^2 k_r^2}{D_s^2}$, characterizes reaction to diffusion rateswhere ϕ \sqrt{Da} is the Thiele modulus, and the functions $h(\gamma)$ and $g(\phi^2)$ are simple Heavyside like functions defined as:

$$h(\gamma) = \begin{cases} 1 & \text{in } \Omega \setminus P, \\ \gamma & \text{in } P. \end{cases}$$
$$g(\phi^2) = \begin{cases} 0 & \text{in } \Omega \setminus P, \\ \phi^2 & \text{in } P. \end{cases}$$

As usual, we can also introduce a Schmidt number $Sc = \frac{\eta^*}{\rho_f^* D_f^*}$ such that Pe Re Sc. Hence the external mass transfer is equivalently characterized by the pair (Re, Pe) or the pair (Re, Sc).

The range of physical quantities are summarized in Table (1) referring to gas solid and liquid solid in industrial applications.

Table 1 Physical properties of industrial gas-solid and liquid-solid reactive particulate systems.

Parameter	Catalyst particle	Liquid	Gas
D (m ² s ¹)	$10^{-6} - 10^{-10}$	$\sim 10^{-9}$	10 6 - 10 5
r_p (mm)	1 – 5	=	-
k_s (s ⁻¹)	$10^{-6} - 10;$	_	_
U_c (cm s ⁻¹)	=	1-2	0.2-20
μ_f (mPa s)		0.386-0.92	~ 0.9
ρ_f (kg m 3)	-	695–770	~ 100

Liquids are hydrocarbons such as Heptane, Decane, or Hexadecane. Gases are a mixture of hydrogen gas and hydrocarbons. According to this table the parameter ranges are: $\gamma \in [0.01,1]$, $\phi \in [0.01,3], Re \in [0,200]$, and $Sc \in [1,1000]$.

2.2. Numerical model

We employ our previously validated Finite Volume/Staggered Grid DLM/FD solver implemented in our code PeliGRIFF. The whole method is fully detailed in Wachs et al. (2015), Rahmani and Wachs (2014) for freely moving particles and in Dorai et al. (2015) for fixed obstacles and was pionneered by Glowinski et al. (1999) in a Finite Element context. We solve the fluid conservation Egs. (9) and (10) on a Cartesian structured mesh of uniform grid size everywhere in the domain (not only in $\Omega \setminus P$ but in the entire Ω) and we enforce motionless obstacles (represented by (11)) in the region (filled with fictitious fluid) occupied by particles using a distributed Lagrange multiplier field. A collocation point method is used to discretize the solid obstacles on the fluid mesh and a second order interpolation of the fluid velocity at the particle boundary (Wachs et al., 2015; Rahmani and Wachs, 2014; Dorai et al., 2015). The strength of our method is that it does not require any kind of hydrodynamic radius calibration (see Wachs et al. (2015) for more details about hydrodynamic radius calibration). The spatial discretization of the diffusive operator in (13) on the non boundary fitted mesh is achieved by a Sharp Interface Method (Fedkiw et al., 1999; Liu et al., 2000; Shao et al., 2012) through which we account for the continuity of C and its normal flux across the fluid/solid interface through the two boundary conditions $[C]_{\partial P}$ 0 and $[h(\gamma)\frac{\partial C}{\partial \mathbf{n}}]_{\partial P}$ 0, respectively. The method is first order accurate in space and it incorporates the jump conditions into the spatial discretization of the diffusive term whereas the other terms in (13) are discretized in a classical way. For the complete imple mentation of the method in 3 D and its validation the reader is referred to Sulaiman et al. (2019b). The overall spatial accuracy of the discretization scheme is however not fully 2nd order due to the non boundary fitted mesh around the solid obstacles. The dimensionless mesh size Δx is related to the number of points per particle diameter through N_p 1/ Δx . N_p can be related to numerical precision by referring to our previous convergence study presented in Sulaiman et al. (2019b). When only transfer is involved the value of N_p is typically 24 to achieve a precision of less than 5% error. To keep the same level of accuracy, the number of grid points per particle diameter is increased to 40 in the presence of chemical reaction which has the tendency to make the boundary layers thinner.

The chemical species problem is one way coupled to the fluid problem through the velocity field \boldsymbol{u} . The discretized conservation Eq. (12) reads as follows for 1^{st} order scheme while the reactive term is treated implicitly:

$$\frac{C^{n+1} C^n}{\Delta t} \nabla \cdot \left(\frac{h(\gamma)}{Pe} \nabla C^{n+1}\right) + \frac{h(\gamma)g(\phi^2)}{Pe} C^{n+1} \\
\frac{1}{2} \left(3\mathbf{u}^{n+1} \cdot \nabla C^n \mathbf{u}^n \cdot \nabla C^{n-1}\right) \tag{13}$$

We solve the full problem as a sequence of a non stationary fluid problem for a given *Re* until the steady state is reached for the Rey nolds numbers we considered. We then follow the fluid problem by a chemical species problem for a given [*Da*, *Sc*] using the computed velocity field until temporal convergence. (see Fig. 1)

2.3. Description of geometry and particles spatial distribution

We consider the simulation domain in Fig. 2 which is uniformly discretized on Cartesian grid. The domain dimensions are set to

 L_x L_y and L_z , which are given in next sections. Particles are ran domly distributed in the packing region $x \in [0, L_x]$, $y \in [0, L_y]$ and $z \in]\Delta I, L_z$ $\Delta I[$, where ΔI is the inlet/outlet zone which is left free of particles. The fluid enters the domain from the bottom boundary with an imposed constant dimensionless velocity $\mathbf{u} = (0,0,1)$ and an imposed concentration C_{∞} 1. Periodic boundary conditions are imposed in x and y directions while a classical outflow bound ary condition $\frac{\partial \mathbf{u}}{\partial z} = \frac{\partial C}{\partial z} = 0$ and $p = p_{ref} = 0$ is imposed at the outlet (top) boundary. In the configuration of packed beds, (Bale et al., 2017) used PRS to characterize the effect of walls that may confine the bed of particles on mass transfer coefficient for low Reynolds number. (Bale et al., 2018) also used PRS to study the inlet and end effects on mass transfer and drew the conclusion that homo geneity of transfer is achieved after two sphere diameters down stream from the bottom of the bed and effect starts from one sphere diameter upstream of the top of the bed. The solid phase consists of catalyst particles experiencing diffusion of the solute and chemical reaction. The solid volume fraction α_s is chosen such that $\alpha_s \in [0.1, 0.5]$ to derive a model which would be valid from the dilute to the dense regime. We consider three values for solid vol ume fraction; $\alpha_s = 0.1(55 \text{ particles}), \alpha_s = 0.3 (165 \text{ particles})$ and 0.5(275 particles), i.e., from a semi dilute regime to a rather dense regime. Up to α_s 0.3, particles are randomly distributed through a random seeding of non overlapping spheres. For 0.5, particles are initially distributed at solid volume fraction α_{si} 0.25, with particles diameter $d_{pi} < d_p$. Then, the particles' radius is expanded. During expansion, particles experience multi ple collisions before they reach the final diameter d_p , that satisfies the desired value of α_s . We use five independent random particle configurations for each mass transfer simulation. According to the convergence study of Sun et al. (2016), this permits to reach a 95% statistical convergence on numerical results. This is consis tent with the spatial resolution N_p we selected ensuring a maxi mum of 5% error.

3. Modeling of mass transfer through assembly of particles

The theoretical modeling is described in this section. First we compare our numerical simulation results to the literature for mass transfer in a random assembly of particles. Then, we consider chemical reaction and present the model for a single particle and extend it to account for solid volume fraction.

3.1. Non reactive mass transfer

The classical way of predicting mass transfer in a two phase fluid solid reactor (catalyst particles undergoing an internal diffu sion reaction, associated to an external convection diffusion) is to decouple the internal and external transfer in the system. Then the two separated problems are coupled at the solid fluid interface, through concentration and flux continuities. Thus, based on the assumption of uniform external mass transfer coefficient, esti mated from correlations on Sherwood number, and using the interface condition, the external and internal transport phenomena are coupled. As a first step, we evaluate the reference Sherwood number in mass transfer controlled regimes, $Da \propto$, i.e. an infinite reaction rate. The system in this case is analogous to heat transfer problem with particles at fixed temperature. We define the cup mixing, or flow averaged concentration as:

$$\overline{C}(z) = \frac{\int_{S_f} u_z(x, y, z) C(x, y, z) dx dy}{\int_{S_f} u_z(x, y, z) dx dy}$$
 (14)

where S_f denotes the cross section area of the fluid and u_z denotes the fluid velocity component along the z direction. Assuming that

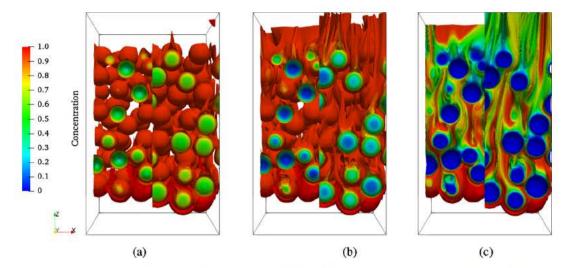


Fig. 1. Concentration isosurfaces for Re 25, Sc 1, γ 0.1, α_s 0.3 and different Damköhler numbers. (a) Da 40, (b) Da 200 and (c) Da ∞ .



Fig. 2. Simulation domain with a random assembly of particles at α_s 0.5.

axial dispersion is negligible, the balance equation for the cup mixing averaged concentration in the system along the z direction is written as follows:

$$\frac{d\overline{C}(z)}{dz} + \xi (\overline{C}(z) \quad C_s) \quad 0 \tag{15}$$

where C_s is the particle concentration and ξ is characteristic of external mass transfer, defined as (16):

$$\xi = \frac{6\alpha_s Sh}{Pe} \tag{16}$$

Hence, the concentration profile along the z direction in the bed, i.e. the solution of (15), is written as:

$$\overline{C}(z) \quad (C_{\infty} \quad C_{\rm s}) exp(\quad \xi z) + C_{\rm s}$$
 (17)

In the above equation the value of ξ can be determined by fitting the concentration profile obtained numerically with the analytical solution (17). α_s and Pe being fixed, the value of ξ obtained by the fitting yields the value of the Sherwood number corresponding to our numerical simulation results.

We perform a set of numerical simulations at constant Sc 1 and Re ∈ [0, 100]. We consider two solid volume fractions α_s 0.1 and α_s 0.3. The particle surface concentration is fixed to zero by setting k_s^* to a very high value that models Da We calculate Sh by fitting numerical simulation results to the 1D model (17). For each (Re, Sc, α_s) we take the average of Sh resulting from 5 different random particle assemblies. The numerical spatial resolution in this case is set to N_p 24 and simulations are per formed at CFL < 0.25 to reach temporal convergence. Domain dimensions are L_x L_y 6, L_z 16, and ΔI 4. We compare the Sherwood number obtained from our simulations with the previ ously established correlations of (Sun et al., 2016; Deen et al., 2014 and Gunn, 1978) in Fig. 3. Our numerical simulation results show higher mass transfer estimate than those of (Deen et al., 2014 and Sun et al., 2016) correlations for α_s 0.1 while a better agreement is observed for α_s 0.3. The numerical results at α_s 0.3 are closer to both correlations than those at α_s 0.1. In both cases the results are below those of (Gunn, 1978) correlation (18), with α_f 1 α_s is the porosity of the bed.

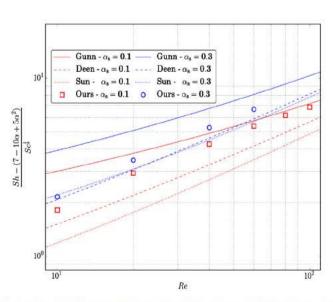


Fig. 3. Comparison of Sherwood number in a random array of particles for external mass transfer with correlations of Gunn (1978), Sun et al. (2016) and ?).

Sh
$$\left(7 \quad 10\alpha_f + 5\alpha_f^2\right)\left(1 + 0.7Re^{0.2}Sc^{1/3}\right)$$

 $+\left(1.33 \quad 2.4\alpha_f + 1.2\alpha_f^2\right)Re^{0.7}Sc^{1/3}$ (18)

We can notice that the numerical simulation results get closer to those of (Gunn, 1978) for both α_s when Re increases.

We show in Fig. A2 (g), (h) and (i) the concentration isosurfaces at infinite reaction rate corresponding to α_s 0.1 and Re 1,10 and 50, respectively.

3.2. Reactive mass transfer: single particle system

We consider a single catalyst particle placed in a convective diffusive fluid stream. The particle experiences internal diffusion coupled to a first order irreversible reaction. The interface conditions of the system are prescribed in (7) and (8). The rest of this section has been detailed in (Sulaiman et al., 2019a) and is summa rized below for the sake of completeness. In (Sulaiman et al., 2019a), the mean particle surface concentration was established as follows:

$$\overline{C_s} = \frac{C_{\infty}}{1 + \frac{\gamma}{Sh} \left(\frac{\phi}{\tanh(\phi/2)} - 2\right)} = \delta C_{\infty}$$
 (19)

Assuming constant C_s , the analytical concentration profile inside the particle is given by:

$$C(r^*) = C_s \frac{r_p^* \sinh(\phi r^*)}{r^* \sinh(\phi r_p^*)}$$
(20)

The mean volume concentration of the particle is obtained by integrating (20)

$$\overline{C_v} \simeq \frac{3}{4\pi r_p^{*3}} \int_0^{2\pi} \int_{\pi/2}^{+\pi/2} \int_0^{r_p^*} C_s(\varphi, \theta) \times \frac{r_p^* \sinh(\phi r^*)}{r^* \sinh(\phi r_p^*)} \sin(\theta) r^{*2} d\varphi d\theta dr^* \tag{21}$$

Assuming C_s uniform over the particle surface, we further approximate the integral as:

$$\overline{C}_{\nu} \simeq \frac{3\overline{C}_{s}}{4\pi r_{p}^{-2}} \int_{0}^{2\pi} \int_{-\pi/2}^{+\pi/2} \int_{0}^{r_{p}} \frac{r_{p}^{*} \sinh(\phi r^{*})}{r^{*} \sinh(\phi r_{p}^{*})} sin(\theta) r^{*2} d\phi d\theta dr^{*}
= \frac{6\overline{C}_{s}}{\phi} \left(\frac{1}{\tanh(\phi/2)} - \frac{2}{\phi}\right) \qquad \beta\overline{C}_{s}$$
(22)

 $\overline{C_s}$ is estimated by (19) and eventually the mean volume concentration $\overline{C_v}$ reads as follows:

$$\overline{C_{\nu}} = \frac{6C_{\infty}}{1 + \frac{\gamma}{Sh} \begin{pmatrix} \frac{\phi}{\tanh(\phi/2)} & 2 \end{pmatrix}} \begin{pmatrix} \frac{1}{\phi \tanh(\phi/2)} & \frac{2}{\phi^2} \end{pmatrix} = \delta\beta C_{\infty}$$
 (23)

with *Sh* is the external Sherwood number. This assumption was validated in (Sulaiman et al., 2019a) for the single particle case, and in (Sulaiman et al., 2019b) for three interacting particles. In the previous cases, the particle *Sh* was evaluated through previously estab lished correlations, such as (Feng and Michaelides, 2000).

3.3. Random assembly of reactive fixed particles

We now consider a system with many particles. All particles have the same physical properties and they are randomly dis tributed, forming a porous network through which the fluid flows. The individual rate of transfer is unknown in this case as the far field or bulk concentration is non uniform. The bulk concentration C(z) varies along the z direction for a network of particles due to the consumption of the chemical species as shown in Fig. 4.

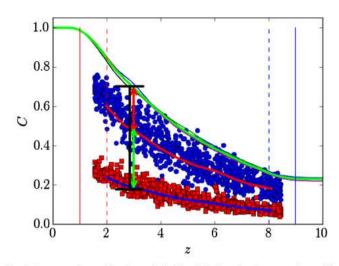


Fig. 4. Concentration profiles along the height of the domain. Green continuous line corresponds to cup-mixing concentration, red line corresponds to average of mean surface concentration and blue line to average of mean volume concentration. Disks correspond to mean surface concentration \overline{C}_s and squares correspond to mean volume concentration \overline{C}_v . Red vertical arrow shows $\Delta \overline{C}_s(z) - \overline{C}_s(z)$, black bar shows $\Delta \overline{C}_v(z) - \overline{C}_v(z) - \overline{C}_v(z)$ and the green vertical arrow shows $\overline{C}_s(z) - \overline{C}_v(z)$. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Thus, the cup mixing, the mean surface and the mean volume concentration profiles need to be predicted along z in order to be able to calculate the internal and external concentration difference. We propose a model using the analogy with the single particle sys tem (19). The key point of the model is to predict the internal and external concentration differences. The external difference is $\Delta \overline{C_s}(z) \quad \overline{C}(z) \quad \overline{C_s}(z)$, between the average cup mixing and mean particle surface concentration. The internal difference between the cup mixing and mean volume concentration is $\Delta \overline{C_v}(z) \quad \overline{C}(z) \quad \overline{C_v}(z)$. We assume that the mean surface concentration of all the particles at a position z is approximated as:

$$\overline{C}_{s}(z) = \frac{\overline{C}(z)}{1 + \frac{\gamma}{Sh} \begin{pmatrix} \phi \\ \tanh(\phi/2) \end{pmatrix}} = \delta \overline{C}(z)$$
 (24)

Sh is the external Sherwood number that can be determined from mass transfer controlled system ($Da \infty$) in a bed of particles. In a single particle system, it was evaluated through existing correlations such as (Feng and Michaelides, 2000) while for a multiparticle system it can be estimated from correlations of (Gunn, 1978) or (Deen et al., 2014) as previously discussed.

Assuming negligible axial dispersion, the equation prescribing the cup mixing concentration profile along the z direction, taking into account the variation of the particle surface concentration along z, writes as follows:

$$\frac{d\overline{C}(z)}{dz} + \xi \left(\overline{C}(z) \quad \overline{C}_s(z)\right) \quad 0 \tag{25}$$

Taking into account the relation in (24), the equation can fur ther be written as:

$$\frac{d\overline{C}(z)}{dz} + \xi(1 \quad \delta)\overline{C}(z) \quad 0 \tag{26}$$

The cup mixing concentration profile $\overline{C}(z)$, accounting for the evolution of the particle concentration as function of z, is simply the solution of (26) and reads as follows:

$$\overline{C}(z) \quad C_{\infty} exp(\xi(1 \delta)z)$$
 (27)

Note that we assumed δ to be constant, $0 < \delta < 1$. For very slow reaction, i.e. $Da \ll 1, \delta \to 1$. For very fast reaction i.e. $Da \to \infty, \delta \to 0$ and (27) is equivalent to (17) with $C_s \to 0$. ξ is the external mass transfer coefficient defined in (16) and is assumed to be independent of reaction rate. To verify the validity of the assumption that the external mass transfer coefficient is independent of Da, we recast (25) in the following form:

$$\xi = \frac{1}{\left(\overline{C}(z) - \overline{C}_s(z)\right)} \frac{d\overline{C}(z)}{dz}$$
 (28)

We compute ξ from numerical simulation results for three values of Da (Da 40, Da 200, and Da ∞) with α_s 0.5, Re 10, Sc 5 and γ 0.1. We compare in Table 2 the min, max, mean and the standard deviation σ of ξ along z. The aver age value of ξ is almost the same for Da 40 and Da 200, with slight decrease for Da ∞ . The calculated results show fluctuations with a standard deviation below 20% or more precisely 12.7% for Da 40, 12.6% for Da 200 and 16% for Da ∞ . This also validates that the assumption of negligible axial dispersion of concentration is valid for Re 10. For higher Reynolds number flows, this assumption will become even more valid.

Now, the mean volume concentration profile along the height z, can be deduced from (22) and (24) as:

$$\overline{C_{\nu}}(z) \qquad \overline{C}(z)\delta\beta \qquad \frac{\overline{C}(z)}{1 + \frac{\gamma}{Sh} \left(\frac{\phi}{\tanh(\phi/2)} - 2\right)} \left(\frac{6}{\phi \tanh(\phi/2)} - \frac{12}{\phi^2}\right) \tag{29}$$

Thus, the cup mixing concentration profile, the mean surface concentration and the mean volume concentration are determined along the height z by (27), (24) and (29), respectively.

4. Numerical simulation results

We perform SIM DLM/FD numerical simulations to validate the model. In this case, we set the simulation domain to: L_x L_y 6, L_z 10, and Δl 1. The spatial numerical resolution is increased to N_p 40 points per particle diameter to increase spatial resolution of boundary layers which are getting thinner with chemical reaction. According to our previous convergence study, performed in (Sulaiman et al., 2019b) for γ 0.1, the numerical error on the surface concentration for the highest Da is less than 5%. All simulations are performed with CFL < 0.25 to reach steady state. All numerical simulation results will be compared to the theoretical modeling in order to test its validity and dependence upon the five dimensionless parameters over the following ranges:

- $\bullet \ \alpha_s \in [0.1, 0.5]$
- $\bullet \ \textit{Re} \in [1, 50]$
- $Sc \in [1, 10]$
- $\bullet \ \textit{Da} \in [40, \infty]$
- $\gamma \in \left[10^{-2}, 10\right]$

Table 2 Statistics on the variation of ξ along z for three values of Da, $\alpha_s = 0.5$, Re = 10, Sc = 5 and $\gamma = 0.1$.

	Da		
ξ	40	200	∞
mean	0.345	0.341	0.33
min	0.332	0.328	0.312
max	0.376	0.371	0.367
σ	0.013	0.013	0.016

The range of parameters corresponds to gas solid systems at low to moderate Reynolds number in order for the flow to remain steady. The ratio of diffusion coefficients models the effects of porosity and tortuosity of the particle micropores. The Schmidt number is limited to 10 because of numerical constraints (higher Schmidt number typical of liquid solid systems would lead to much thinner mass boundary layer). The range of Schmidt numbers [1,10] considered corresponds, e.g., naphtalene air system (Sc 2.5). We compare the predictions of the model for the con centration profiles $\overline{C}(z)$, $\overline{C}_s(z)$, and $\overline{C}_v(z)$, corresponding to (27), (24) and (29), respectively, with our numerical results.

We compute $\overline{C}_s(z)$ numerically by sub dividing the bed along z into 10 slabs, indexed by i,i from 1 to 10. In slab i, we define n as the number of particles whose centers lie in the slab, \overline{C}_{spj} the mean surface concentration of a particle j (j from 1 to n), and \overline{Z}_{spj} the average particle position along z. We compute the average of mean surface concentration of all the particles in the slab i as follows:

$$\overline{C_{si}} = \frac{1}{n} \sum_{i=1}^{n} \overline{C_{spj}}$$
 (30)

We compute the corresponding \overline{z}_{si} position for \overline{C}_{si} as follows:

$$\overline{Z_{si}} = \frac{1}{n} \sum_{j=1}^{n} \overline{Z_{spj}}$$
 (31)

We follow the same procedure for the calculation of the average of mean volume concentration. For each case, we take the average of the five simulations corresponding to different random particle assemblies.

We consider three values for solid volume fraction; $\alpha_s = 0.1(55 \text{ particles})$, $\alpha_s = 0.3$ (165 particles) and $\alpha_s = 0.5(275 \text{ particles})$, i.e., from a semi dilute regime to a rather dense regime.

4.1. Dilute regime (α_s 0.1)

We present different cases with increasing effect of convection, the Reynolds number is varying from 1 to 10 while Schmidt num ber is either equal to 1 or 10. For each configuration, the effect of the kinetics of the chemical reaction is tested with two values of Damköhler number Da-40 and Da-200. Finally, we investigate the modulation of mass transfer rate by the ratio of diffusion coefficients γ .

- Case A, we fix γ 0.1, Re 1, Sc 1 for two values of Da:Da 40 and Da 200.
- Case B, we fix γ 0.1, Re 1, Sc 10 for two values of Da:Da 40 and Da 200.

In case A, we compare the models at low Re, low α_s and low Sc. We only vary Da. Then, in case B, the value of Sc is increased from 1 to 10, with respect to case A, which leads to higher Peclet number (Pe Re.Sc). We show the comparison between the predictions of our model and our numerical simulation results in Fig. 5 for the two cases. The predictions of our model com pare well with our numerical results with a weaker agreement when Sc 10 and Da 200, corresponding to thin external and internal boundary layers which scale with Sc $^{1/3}$ and Da $^{1/2}$, respectively. It is clear that the observed discrepancy is stronger on profiles of $\overline{C_s}(z)$ and more specifically when both Sc and Da are large (the largest discrepancy being below 20%).

- Case C, we fix γ 0.1, Re 10, Sc 1 for two values of Da:Da 40 and Da 200.
- Case D, we fix γ 0.1, Re 10, Sc 10 for two values of Da:Da 40 and Da 200.

In cases C and D, we only increase the value of Re from 1 to 10.

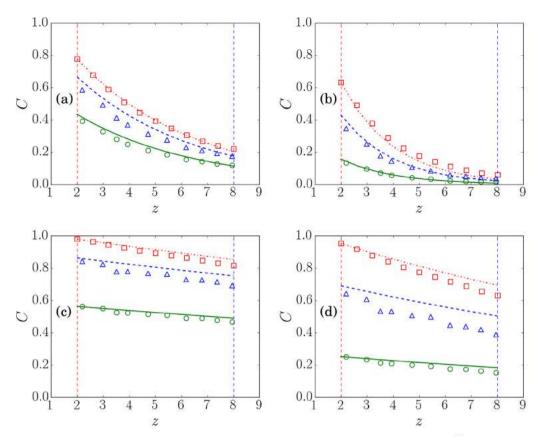


Fig. 5. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.1$, Re = 1, and $\gamma = 0.1$. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, and (a) correspond to C(z) and (b) correspond to C(z) and (c) correspond to C(z) and (c) correspond to C(z) and (d) correspond to C(z) and (e) correspond to C(z) and (f) correspond to C(z) and (g) correspond to

We show the comparison between the predictions of our model and our numerical simulation results in Fig. 6. The numerical results show a very good agreement between our model and the numerical results although the model overpredicts $\overline{C_s}(z)$ in Fig. 6 a and b. Concentration profiles decrease with a lower slope along the height compared to cases A and B. This is due to the increase of convective effects induced by an increase of Re from 1 to 10. Mass transfer evolves with $Re^{1/3}$ which enhances solute supply at particles interface and convective transport through the random assembly of particles. For case D, the concentration variation is very weak along the height. This is the result of great enhancement of the Peclet number (Pe-500) while reactive effect remains moderate.

- Case E, we fix γ 0.1, Re 50, Sc 1 for two values of Da:Da 40 and Da 200.
- Case F, we fix γ 0.1, Re 50, Sc 10 for two values of Da:Da 40 and Da 200.

In cases E and F, and with respect to cases C and D, we only increase the value of *Re* from 10 to 50. We show the comparison between the predictions of our model and our numerical simula tion results in Fig. A1. The numerical results show a very good agreement between the predictions of our model and our numerical results. Concentration profiles decrease with a lower slope along the height than cases A, B, C and D which correspond to higher *Pe* number (e.g. 50 and 500). This is due to the increase of convective effects related to the increase of *Re* at constant reaction rate and constant solid volume fraction. At higher Peclet number,

the dimensionless transfer coefficient is expected to scale with $Pe^{1/3}$.

• Case G, we fix Re = 50, Sc = 10, and Da = 40 which corresponds to strong convection Pe = 500 and moderate reaction kinetics. We vary γ such that $\gamma = \left[10^{-2}, 10^{-1}, 1, 10\right]$.

Finally, in the dilute regime, we vary in case G the diffusion coefficient ratio γ (γ 0.1 was kept constant in all other simula tions). For this case, we fix Re 50, Da 40, Sc 10, and α_s 0.1. We compare the predictions of our model and our numer ical results for four values of γ : 10 2 , 10 1 , 1, and 10. We compare results in Fig. 7. For γ 10 ² and γ 10 ¹, the predictions of our model show a very good agreement with our numerical simulation results. For y 1, numerical results show a systematic deviation from the predictions of the model. The difference between the pre dictions of the model and the numerical simulation results increases for γ 10. It is markedly large for $\overline{C_s}(z)$ which is under predicted by a factor almost 2. Increasing the diffusion coefficient ratio y at a constant Da decreases the surface and mean volume concentration of the particles (see Fig. 8). However, this configura tion of higher diffusion in particles is not likely to occur in practical applications.

In fact, decreasing the bulk diffusion coefficient decreases the supply of chemical species to particles, at a constant consumption rate of reaction. This is in line with what takes place when Re or Sc is decreased. Mathematically, γ tending to ∞ in (24) or ϕ $Da^{1/2}$ tending to ∞ in (24) has the same effect. In both cases the particle surface concentration tends to zero and thus the internal boundary layer gets thinner.

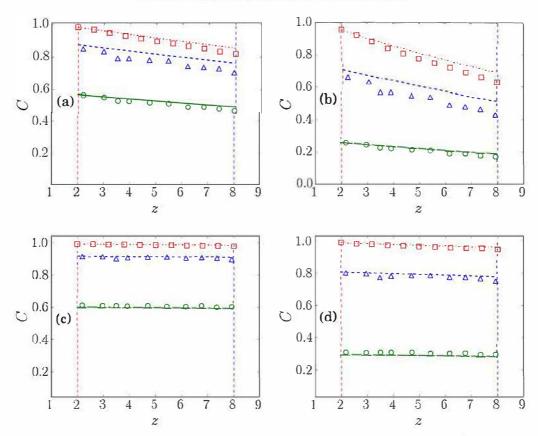


Fig. 6. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.1$, Re = 10, and $\gamma = 0.1$. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$. Lines stand for model and symbols for simulations. (a) and (b) correspond to Sc = 1, (c) and (d) correspond to Sc = 10, (a) and (c) correspond to Da = 10. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

In order to illustrate this observation, we arbitrarily select five particles in the assembly and we plot their internal concentration profiles for $\gamma=10^{-2}, \gamma=1$ and $\gamma=10$ in Fig. 9. When the diffusion ratio is lower than one, it models the reduction of the diffusion coefficient due to confinement in the micropores of the porous cat alyst particle. Increasing the diffusion ratio above one shifts pro gressively the main resistance to transfer from the internal to external boundary layer. We give information on the positions of the selected particles in Table 3.

Particles show approximately a similar concentration profile for the same γ for all positions. However, when γ increases, the surface concentration significantly decreases with an increase of the gradi ent between the surface and bulk concentrations. This explains the increase of the numerical error and thus the model cannot be tested in this case as the simulations are not well spatially resolved. The concentration iso contours of this case are shown in Fig. 8. They clearly show the decrease of the particle concentra tion with an increase of y. This observation is similar to what we can see in Fig. 11, where we compare the concentration iso contours for another case at Re 25, γ 0.1, Sc 10, α_s 0.3 and many Da. We show in Fig. A2 the concentration iso surfaces for $\alpha_s = 0.1$, $\gamma = 0.1$ and Sc = 1. In (a), (b) and (c), we increase Re from 1, to 10 and 50 respectively, at a constant Da. The concentra tion increases with the increase of Re. As previously pointed out, the increase of Re increases the convective effects and solute sup ply at constant consumption rate. In Fig. A2 (c), (f), and (i), Re is fixed to 50 and the reaction rate increases such that 40, 200 and ∞. The mean solute concentration in particles as well as the mean concentration in the fluid decrease with an increase of Da. At a constant supply rate through convection and mass diffusion, the consumption of the chemical species due to reaction has been increased. The increase of Da increases significantly the slope of concentration gradients near particle surfaces. This is the reason why we selected N_p 40 grid points per particle diameter in order to accurately capture the correct boundary layers (while for external mass transfer only N_p 24 was sufficient for a similar level of accuracy). Thus, we infer that the discrepancy between the model and simulations when we increase γ is due to the numerical spatial resolution.

4.2. Moderately concentrated regime (α_s 0.3)

- Case H, we fix $\gamma = 0.1, Re = 10, Sc = 1$ for two values of Da:Da = 40 and Da = 200.
- Case I, we fix γ 0.1, Re 10, Sc 10 for two values of Da: Da 40 and Da 200.

In cases H and I, we only increase the solid volume fraction α_s from 0.1 to 0.3 with respect to cases C and D. Increasing the solid fraction in the bed yields reduction of the mean interparticle dis tance which scales with α_s ^{1/3}. We show the comparison between the predictions of our model and our numerical results in Fig. 10. The numerical simulation results show a good agreement between the predictions of our model and our numerical results for Sc 1 although it is clear that the discrepancy is stronger on profiles of $\overline{C_s}(z)$. The agreement gets better for Sc 10. The physical explanation of this observation is that when the convective effects increase, the particle surface concentration gets more uniform, and so, the assumptions made to obtain (24) are more valid. Indeed, for a given particle in the bed, neighboring particles induce heterogeneity to its surrounding concentration field. The increase of Re or Sc, consequently Pe Re.Sc, enhances the uniformity of

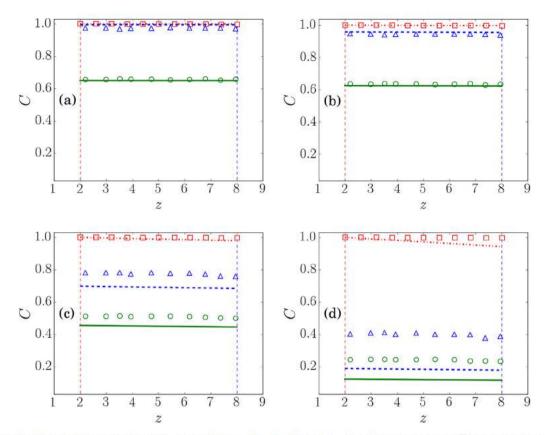


Fig. 7. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.1$, Re = 50, and Da = 40. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}_s(z)$ and green color corresponds to $\overline{C}_s(z)$. Lines stand for model and symbols for simulations. (a) corresponds to $\gamma = 0.01$, (b) corresponds to $\gamma = 0.1$, (c) corresponds to $\gamma = 1$ and (d) corresponds to $\gamma = 1$. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

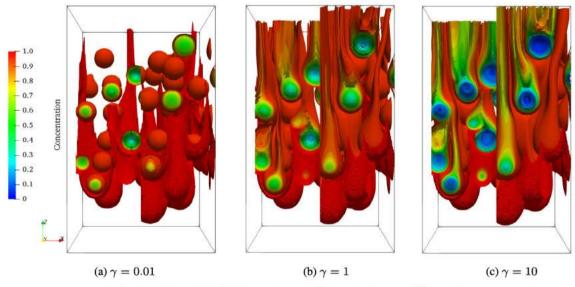


Fig. 8. Concentration contours at Re 50, Sc 10, Da 40, α_s 0.1, γ 10^{-2} , 1 and 10.

the concentration field. Assuming $Pe \to \infty$, the concentration field around the particle will be uniform and equal to the inlet concentration C_{∞} .

Concentration profiles decrease with a lower slope along the height than in cases C and D. This is due to the increase of the num ber of particles per volume of reactor and consequently an increase of the specific surface available for chemical reaction which induces stronger consumption of the solute concentration. An

increase of the reaction kinetics yield significant local inhomo geneities of concentration distribution across the bed (see Fig. 11).

4.3. Dense regime (α_s 0.5)

• Case J, we fix γ 0.1, Re 1, Sc 1 for two values of Da:Da 40 and Da 200.

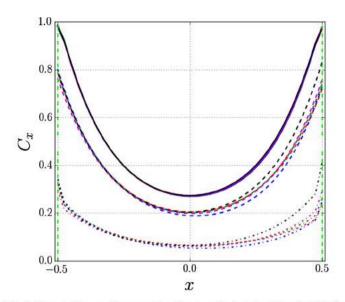


Fig. 9. Concentration profiles across the diameter of selected particles in Table 3. Continuous lines correspond to $\gamma=10^{-2}$, dashed lines correspond to $\gamma=10^{-1}$ and dotted lines correspond to $\gamma=10$. Colors: magenta, blue, green, black, and red correspond to particles (a), (b), (c), (d), and (e.), respectively. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 3Positions of selected particles in the bed for concentration profiles comparison shown in Fig. 9.

Particle	Position		
	x/d	y/d	z/d
a	4.872	2.499	1.701
b	5.706	4.04	3.309
С	5.948	5.500	5.946
d	5.933	3.611	7.057
e	2.411	2.334	7.447

• Case K, we fix γ 0.1, Re 1, Sc 10 for two values of Da:Da 40 and Da 200.

Cases I and K are similar to cases A and B, but with an increase of the solid volume fraction α_s from 0.1 to 0.5. We show the com parison between the predictions of our model and our numerical simulation results in Fig. 12. The results show a good agreement between the predictions of our model and our simulation numeri cal results for both Sc 1 and Sc 10 (the discrepancy is stronger on profiles of $\overline{C_s}(z)$ when the Sc number is large). However, model predictions are better for cases A and B (where $\alpha_s = 0.1$). When solid volume fraction increases, the surface concentration of a given particle experiences non uniform spatial distribution of the surrounding concentration field. The presence of many neighbor ing particles strongly disturbs the concentration field and so the assumption made in (24) is less valid. This is especially significant when convective effects are weak corresponding to thick boundary layers. Concentration profiles in these cases show a steeper slope along the height than in cases A and B. This is due to an increase of number of particles and consequently an increase of the mean consumption rate of the chemical species over a certain height.

- Case L, we fix γ 0.1, Re 10, Sc 1 for two values of Da:Da 40 and Da 200.
- Case M, we fix γ 0.1, Re 10, Sc 5 for two values of Da:Da 40 and Da 200.

Cases L and M are similar to cases J and K, with an increase of *Re* from 1 to 10. (Note that *Sc* 5 in case M whereas *Sc* 10 in case K.) We show the comparison between the predictions of our model and our numerical results in Fig. 13.

The numerical simulation results show an overall good agree ment between the predictions of our model and our numerical results for both Sc 1 and Sc 5 while the discrepancy is stronger on profiles of $\overline{C_s}(z)$. However, the predictions of the model are bet ter in cases L and M than in cases J and K. For a given solid volume fraction, the particle surface concentration becomes more uniform when the convective effects increase. The increase of the convective effects enhances the spatial homogeneity of the concentration field and reduces the disturbances induced by neighboring particles. Hence, the assumption made in (24) is more valid. Concentration profiles have a lower slope along the bed height than in cases J and K. This is due to the increase of convective supply of chemical species to the particles surface at a constant consumption rate.

- Case N, we fix γ 0.1, Re 25, Sc 1 for two values of Da:Da 40 and Da 200.
- Case O, we fix γ 0.1, Re 25, Sc 10 for two values of Da: Da 40 and Da 200.

Cases N and O are similar to cases L and M, with only an increase of Re from 10 to 25. (Note that Sc 10 in case O whereas 5 in case M.) We show the comparison in Fig. A3. We observe a good agreement between the predictions of our model and our numerical simulation results for both Sc 1 and Sc the prediction of profiles of $\overline{C_s}(z)$ is less accurate. However, the pre dictions of the model are almost similar to those in cases L and M although a systematic overestimate of $\overline{C}_s(z)$ is observed. Increasing convective effects does not change the level of agreement between the predictions of the model and the numerical simulation results. In all cases where α_s 0.5, the agreement between the predictions of the model and the numerical results is weaker. The assumptions are less valid at high solid volume fraction. Particles may experi ence, in this case, strong spatial concentration variations over their surfaces due the disturbance induced by neighboring particles. Serious limitations of the model were expected in this case due to strong inhomogeneities of the concentration field across the assembly of particles.

5. Dimensionless mass transfer coefficient

5.1. Reactive Sherwood number

For a single particle, the mass transfer coefficient that accounts for all the effects in the system can be obtained through the additivity rule. The rule states that the total resistance to mass transfer in the system can be considered as a sum of two resistances in ser ies. The first resistance is the inverse of the internal mass transfer coefficient k_{in}^* in the solid phase, and the second resistance is the inverse of the external transfer coefficient k_f^* in the fluid phase. The total mass transfer coefficient k^* , via the additivity rule, writes as:

$$\frac{1}{\bar{k}^*} \quad \frac{1}{k_{in}^*} + \frac{1}{k_f^*} \tag{32}$$

We consequently introduce two Sherwood numbers as:

internal Sherwood number Shin

$$Sh_{in} \quad \frac{N_{s,\partial P}^* d_p^*}{D_s^* (\overline{C_s} \quad \overline{C_v})} \quad \frac{k_{in}^* d_p^*}{D_s^*} \tag{33}$$

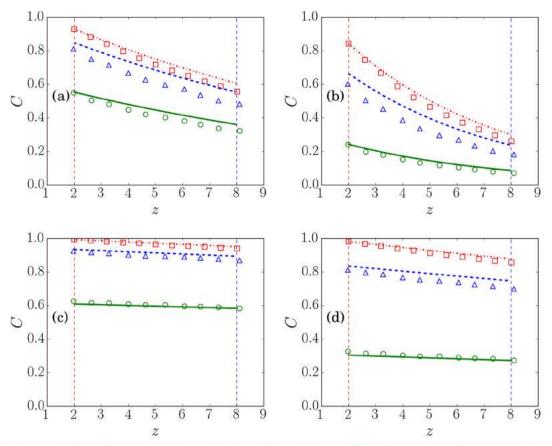


Fig. 10. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.3$, Re = 10, and $\gamma = 0.1$. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, and $\overline{C}(z)$ and \overline

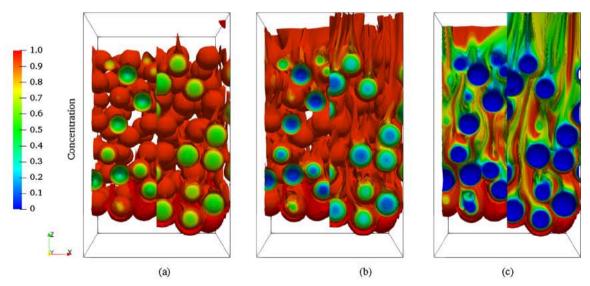


Fig. 11. Concentration contours at Re 25, γ 0.1, α_s 0.3 with (a) Da 40, (b) Da 200 and (c) Da ∞ .

• external Sherwood number Sh

We reformulate (32) in terms of Sherwood numbers. The global Sherwood number for an isolated particle $\widetilde{Sh_0}$ $\frac{k^* d_p^*}{D_f^*}$, is obtained from:

$$Sh \quad \frac{N_{f,\partial P}^* d_p^*}{D_f^* \left(C_{\infty} \quad \overline{C_s}\right)} \quad \frac{k_f^* d_p^*}{D_f^*} \tag{34} \qquad \frac{1}{\widetilde{Sh_o}} \quad \frac{1}{\gamma Sh_{in}} + \frac{1}{Sh} \tag{35}$$

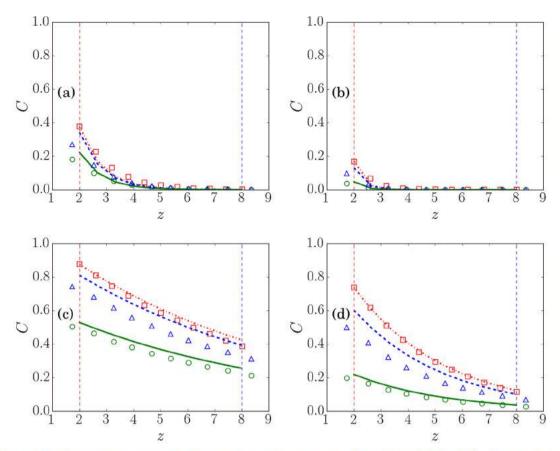


Fig. 12. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.5$, Re = 1, and $\gamma = 0.1$. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$. Lines stand for model and symbols for simulations. (a) and (b) correspond to Sc = 1, (c) and (d) correspond to Sc = 10, (a) and (c) correspond to Da = 10, (a) and (b) and (d) correspond to Da = 10. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Sh was evaluated through previously established correlations, such as (Feng and Michaelides, 2000) for an isolated particle. The expression of $\widetilde{Sh_o}$ can be written as function of Sh, $\Delta \overline{C_s}$ C_{∞} $\overline{C_s}$ and $\Delta \overline{C_v}$ C_{∞} $\overline{C_v}$, using the continuity of the flux density at ∂P , it reads as follows:

$$\widetilde{Sh_0}$$
 $Sh\frac{C_{\infty}}{C_{\infty}}$ $\overline{C_v}$ $Sh\frac{\Delta \overline{C_s}}{\Delta \overline{C_v}}$ (36)

Using (19) and (22), the reactive Sherwood number Sh_0 of the single sphere system can be written as:

$$\widetilde{Sh_o}(Re,Sc,\phi,\gamma) = \frac{Sh(Re,Sc)}{\frac{Sh(Re,Sc)}{2\gamma} \left[\frac{\tanh(\phi/2)}{\phi/2 \tanh(\phi/2)} \frac{12}{\theta^2}\right] + 1}$$
(37)

In the case of a bed of particles with solid concentration α_s , the global mass transfer coefficient is obtained with

$$\widetilde{Sh}(Re, Sc, \phi, \gamma, \alpha_s) = Sh \frac{\Delta \overline{C_s}(z)}{\Delta \overline{C_v}(z)} = Sh \frac{\overline{C}(z)}{\overline{C}(z)} \frac{\overline{C_s}(z)}{\overline{C_v}(z)}$$

$$Sh \frac{\overline{C}(z)}{\overline{C}(z)} \frac{\delta \overline{C}(z)}{\delta \beta \overline{C}(z)} = Sh \frac{1}{1} \frac{\delta}{\delta \beta}$$
(38)

In the case of a bed of particles, Sh was obtained by our simula tions with infinite Da (see for example Fig. 3) or can be approximated by correlation (18) of (Gunn, 1978). This expression accounts for the overall solid fraction α_s in the bed but neglects direct particle interactions mediated by the fluid (all particles at a given height are assumed to have similar concentration).

This dimensionless coefficient includes the coupled effects of external diffusion convection and internal diffusion reaction on the overall mass transfer from the particles to the fluid. This can be used, for instance, as a closure law for reactive mass transfer simulations in DEM CFD (DEM stands for Discrete Element Meth ods) approaches for which mass balance equations are resolved at a much larger scale than the particle size. Our micro to meso scale modelling is tested under different configurations from the dilute to the dense regime. The expression of \widehat{Sh} which formally does not depend on z is based on the assumption that all particles at the same height in the bed must behave uniformly (same surface concentration which is an assumption to be tested similarly to Table 2). We compare the reactive Sherwood number \widehat{Sh} (38) with numerical simulations for four different cases with γ 0.1:

- I: α_s 0.1, and Sc 1.
- II: α_s 0.1, and Sc 5.
- III: α_s 0.1, and Sc 10.
- IV: α_s 0.5, and Sc 10.

In the first three cases, I, II and III, we fixed $\alpha_s=0.1$ and Sc varies from 1 to 10. For each case we consider three values of Da $(40,200,\infty)$ and two values of Re (10,50). For the fourth case, IV, we consider $\alpha_s=0.5$ and Sc=10, three values of Da $(40,200,\infty)$ and two values of Re (10,25). We show the results in Fig. 14. For the first three cases, I, II and III, the predictions of the model compare well with the numerical simulation results. However the predictions of the model are better in case II than in case I, and better in case III than in case II. In case IV, the predictions of the model

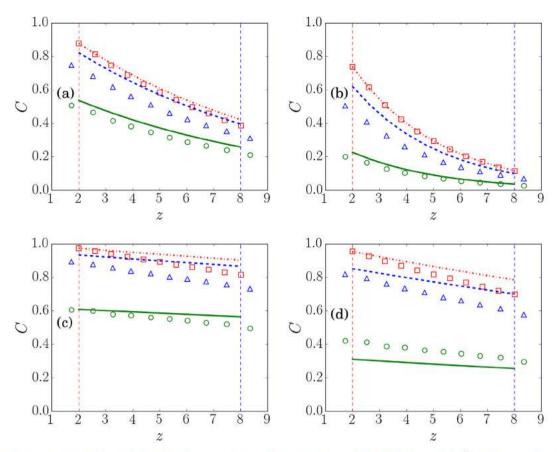


Fig. 13. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.5$, Re = 10, and $\gamma = 0.1$. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, and (b) correspond to Sc = 1, (c) and (d) correspond to Sc = 5, (a) and (c) correspond to Sc = 6, (a) and (b) and (d) correspond to Sc = 6, (a) and (c) correspond to Sc = 6, (b) and (c) correspond to Sc = 6, (c) and (d) correspond to Sc = 6, (e) and (f) correspond to Sc = 6, (f) and (f) correspond to Sc = 6, (e) and (f) correspond to Sc = 6, (f) and (f) correspond to Sc = 6, (e) and (f) correspond to Sc = 6, (f) and (f)

show a weaker agreement with the numerical results. Note that the only difference between case III and case IV is the solid volume fraction, i.e., otherwise all other dimensionless parameters are the same in both cases.

5.2. Discussion

The reactive Sherwood number is a dimensionless quantity characterizing the rate of mass transfer while a chemical reaction takes place within catalyst particles.

At high α_s and low Pe, we observe that the semi-analytical predictive model shows limitations. The assumption for the prediction of the mean surface concentration of the particles is that the local particle surface concentration does not experience important vari ations due to hydrodynamic perturbations of surrounding particles (this is expected to be true for a dilute system). Consequently, the model is expected to show limitations when the local surface con centration of each particle is non uniform due to local heterogene ity of the concentration spatial distribution generated by mass boundary layers and wakes. When the solid volume fraction increases, more particles are interacting with each other through out the assembly. However, the homogeneity of the concentration spatial distribution is enhanced when Pe increases. Indeed, increas ing Pe strengthens convective effects and consequently enhances supply of chemical species to the bed which is consumed by parti cles. Assuming an infinite flow rate (for any given α_s), the concen tration field surrounding each particle will tend to uniform concentration C_f C_{∞} .

In order to elaborate on model limitations, we compute the standard deviation σ of the normalized cup mixing concentration

distribution (Eq. (39)) over the bed for two sets of simulation: vary ing *Pe* through different Reynolds number at *Sc* 10 and varying the solid volume fraction while other parameters are kept constant.

$$\kappa = \frac{C_f(x, y, z) - \overline{C}(z)}{\overline{C}(z)} \tag{39}$$

The mean of the standard deviation is formed over the five ran dom seeding of particles and characterizes the homogeneity of the spatial distribution of solute concentration.

First, when the solid volume fraction is fixed, α_s 0.1, we investigate the effect of convection (see Table 4). For Re 50, the standard deviation σ is very low corresponding to rather uniform distribution of the concentration. Reducing Re to 10 and 1, σ increases drastically. This emphasizes that the concentration field is getting more and more heterogeneous when Re decreases, as expected. The case Re 10 is illustrated on the left column of Fig. 15.

In the second set of simulations (see Table 5), we fix Re 10 and Sc 10 while the solid volume fraction is varied from dilute to dense regime. For α_s 0.1, σ is small while it increases for α_s 0.3, and even more for α_s 0.5. This shows that the concentration field is getting more heterogeneous when the number of particles in the assembly increases and that interparticle distance reduces. This results from direct pairwise or multibody particle interactions mediated by the fluid flow. The concentration and velocity magnitude spatial distributions in a horizontal slice are shown at mid height, z 5d, in Fig. 15, for Re 10, Sc 10, Da 200, γ 0.1 and two values of solid fraction

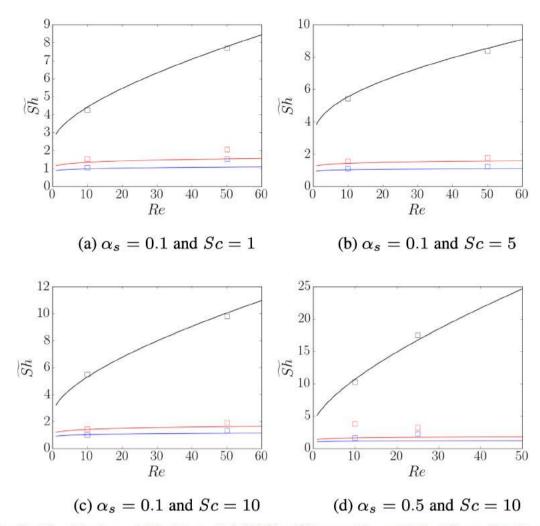


Fig. 14. Comparison of model prediction to numerical simulation results. (a), (b), (c), and (d) correspond to cases I, II, III, and IV, respectively. Colors blue, red and black correspond to Da = 40, Da = 200 and $Da = \infty$, respectively. Continuous lines represent model and symbols represent simulations. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Table 4 The standard deviation σ of (39) for $\gamma=0.1, Da=200, \alpha_s=0.1, Sc=10$ and different Re corresponding to Pe equal to 10, 100 and 500.

Configurations	$\sigma_{Re=1}$	$\sigma_{Re=10}$	$\sigma_{Re=50}$
Mean value	0.2474	0.1628	0.0936

 α_s (0.1 and 0.3). We can clearly observe that the concentration field heterogeneity is increased when α_s increases due to the presence of neighboring particles. The spatial distribution of the concentration for both α_s is strongly correlated to the velocity magnitude which is enforced by the presence of no slip boundary condition on particle surfaces. In fact, this is a direct effect of the local microstruc ture of the assembly due to the relative position of particles. In the model, these direct hydrodynamic interactions are neglected and only the solid volume fraction is accounted for in the correlation.

6. Conclusion

We studied the effect of a first order irreversible chemical reaction on mass transfer through random assemblies of reactive spherical catalyst particles. We derived a theoretical model for the prediction of the cup mixing concentration profile of the fluid, the average of mean surface and the average of mean volume con

centration profiles of the catalyst particles assuming axial disper sion is negligible. The model we proposed accounts for the effects of convection and diffusion in the fluid phase along with diffusion and chemical reaction in the solid phase. Under steady state, the model assumes that internal and external mass transfers can be coupled through continuity of concentration and flux den sity at the particle surface. Assuming constant and uniform con centration distribution along the surface of each particle, internal transfer coefficient is calculated through an analytic solution of diffusion reaction mass balance equation inside particles.

We performed particle resolved numerical simulations over a wide range of the five dimensionless parameters controlling the system ($Re, Sc, \alpha_s, \gamma, Da$) and we compared the predictions of our model to our numerical simulation results. The model showed a very good ability to predict the correct concentration profiles resulting from numerical results. Also, the dimensionless mass transfer coefficient is well predicted by our model of 'reactive' Sherwood number. At a constant Pe, the model has proven to better predict the profiles when the solid volume fraction α_s decreases. Conversely, at a constant α_s , the predictions of the model improved when Pe increases.

The limitations of the model at high solid volume fraction and low convective effect arise from the fact that the model for the mean surface concentration of the particle was derived assuming that the particle surface concentration does not experience any sig

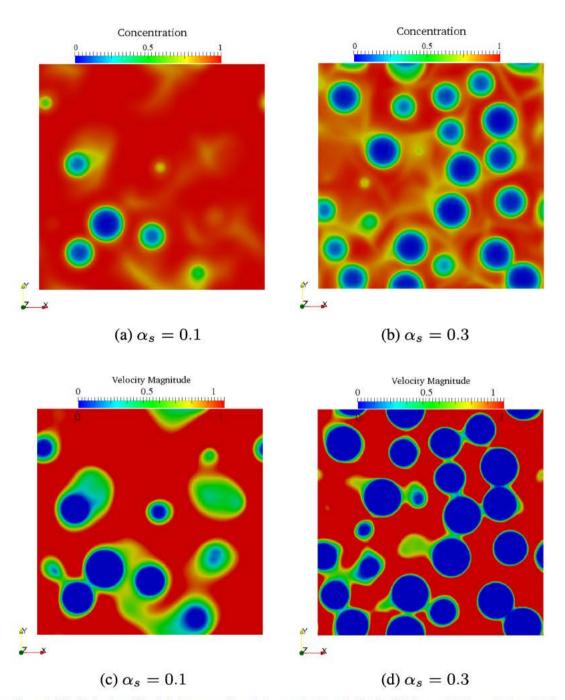


Fig. 15. Concentration spatial distribution (a and b) and their corresponding velocity magnitude (c and d) in the mid-plane z 0.5, for γ 0.1, Da 200, Re 10 and Sc 10

Table 5 The standard deviation σ of (39) for γ 0.1, Re 10, Da 200, Sc 10 and different volume fractions α_s .

Configuration	$\sigma_{\alpha_i=0 \ 1}$	$\sigma_{\alpha_i=0.3}$	$\sigma_{\alpha_s=0.5}$
Mean value	0.072	0.259	0.7508

nificant spatial variation. This assumption has been shown to be valid for a system comprising a single particle or three interacting aligned particles, since the concentration field around each particle is quasi uniform in these cases. Moreover, it is assumed in the model that all particles at a certain height in the bed have the same concentration. Chemical species are consumed by the particles and in each wake there is a local reduction of solute concentration

which is transported by the fluid. When the solid volume fraction increases, more particles are present in the system, inducing heterogeneities to the concentration field due to their consump tion of the chemical species transported by the fluid, that in turn affects negatively the surface concentration uniformity of particles. Indeed, at high concentration of particles local hydrodynamic interactions yield strong inhomogeneities of the solute concentration spatial distribution. The surface concentration on neighboring particles is strongly influenced by the local concentration variations in the bulk of the fluid. This is particularly true at low *Pe* number. This makes the assumption of uniform solute surface distribution far from being valid and flaws the prediction of the model. The local particle interactions mediated by the fluid makes the concentration of particles to be non uniform at a given height

while the model only accounts for the overall solid fraction of the dispersed phase. This is a strong limitation of the model towards denser regimes.

When Pe increases, convective effects increase and the fluid transports more chemical species to the system at a constant con sumption rate by the particles. This enhances the uniformity of the concentration field around particles, that tends to be equal to the inlet concentration at infinite flow rate, i.e. $Pe \to \infty$. This observation has been confirmed by analyzing statistics of the distribution of cup mixing concentration for different solid volume fractions and different Peclet numbers. However, moving to very high Peclet numbers (very often because of large values of the Schmidt number in liquids, see for example (Bale et al., 2019) where the effect of Schmidt number was investigated on transfer in packed beds) would yield stronger constraints on the numerical spatial resolution of the thin boundary layers and wakes around particles. The number of points per particle diameter becomes very soon prohibitive for direct numerical simulations as it scales with $Pe^{-1/3}$.

Future work aims at addressing the extension of the established model to more complicated reaction kinetics (higher order) and reversible chemical reactions or multi species and multi reactions systems. This will involve finding the analytical solutions of concentration profiles within the catalyst particles in order to perform the internal external coupling. This will give information on enhancing the prediction of performances for realistic fixed or fluidized bed catalytic reactors. The current model is also to be coupled to heat transfer (Lu et al., 2019) to account for temperature

effect on reaction rate (exothermic reactions) and fluid density variations leading to natural convection effects. The current work represents a first step towards a general model for the 'reactive' Sherwood number in dense particulate flow systems with a first order chemical reaction. Upcoming efforts in terms of theoretical modeling can include axial dispersion of the reactants and prod ucts along the bed. Upcoming work also necessitates performing a multi scale micro meso comparison to test the performance of the model as a closure law for meso scale systems.

Declaration of Competing Interest

The authors declare that they have no known competing finan cial interests or personal relationships that could have appeared to influence the work reported in this paper.

Acknowledgments

This work was granted access by GENCI to the HPC resources of CINES under the allocations 2016 c20132b6699 and 2017 c20142b6699. This study is part of the ANR collaborative project More4Less (IFP EN, CORIA, IMFT and UBC).

Appendix A

Figs. A.1 A.3.

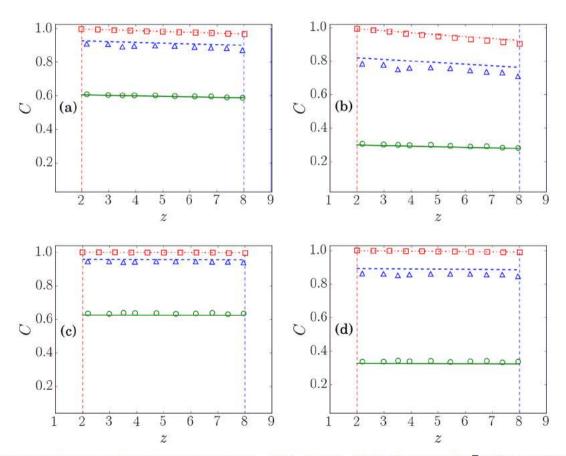


Fig. A1. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.1$, Re = 50, and $\gamma = 0.1$. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$. Lines stand for model and symbols for simulations. (a) and (b) correspond to Sc = 1, (c) and (d) correspond to Sc = 10, (a) and (c) correspond to Da = 200. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

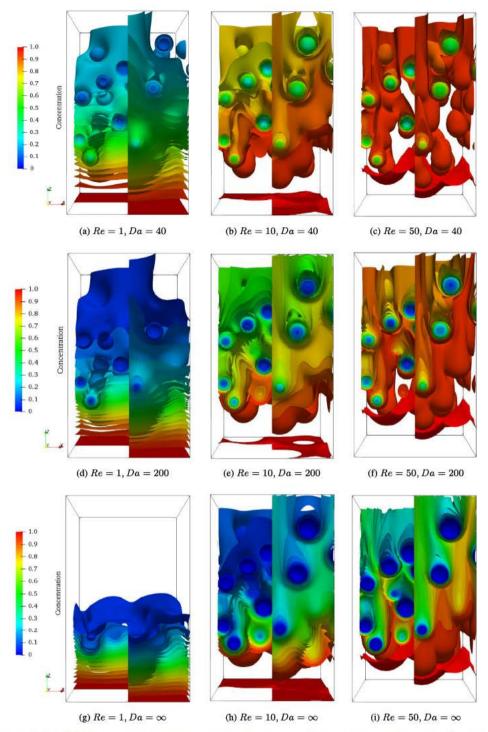


Fig. A2. Visualization of the interplay between convection, diffusion, and chemical reaction. Concentration isosurfaces for $Sc=1, \gamma=0.1$ and $\alpha_s=0.1$. From left to right, convection increases. From top to bottom, reaction rate increases. Along the diagonal from left-top to right-bottom both convection and reaction rate increase.

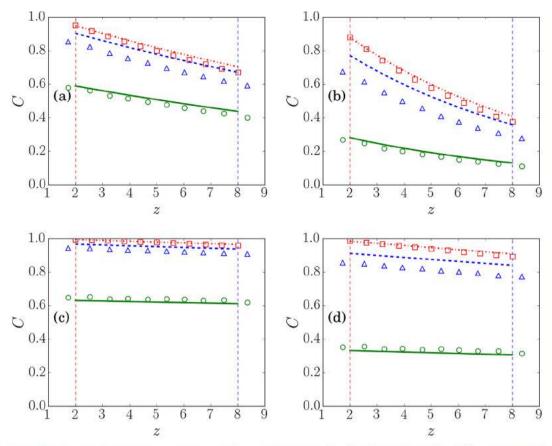


Fig. A3. Comparison of model prediction to numerical simulation results for $\alpha_s = 0.5$, Re = 25, and $\gamma = 0.1$. Red color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$, blue color corresponds to $\overline{C}(z)$. Lines stand for model and symbols for simulations. (a) and (b) correspond to Sc = 1, (c) and (d) correspond to Sc = 10, (a) and (c) correspond to Sc = 10, (a) and (b) and (c) correspond to Sc = 10, (a) and (c) correspond to Sc = 10, (b) and (c) correspond to Sc = 10, (c) and (d) correspond to Sc = 10, (e) and (f) and (g) correspond to Sc = 10, (e) and (f) and (g) correspond to Sc = 10, (e) and (f) and (g) correspond to Sc = 10, (e) and (f) and (g) correspond to Sc = 10, (e) and (f) and (g) correspond to Sc = 10, (e) and (f) and (g) correspond to Sc = 10, (f) and (g) correspond to Sc = 10, (g) and (g) correspond to Sc = 10, (e) and (f) correspond to Sc = 10, (f) and (g) correspond to Sc = 10, (g) and (g)

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