

CFD Simulation for Characterization and Scale-Up of Pulsed Biomass Transport

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► To cite this version:

Lucas Massaro Sousa, Benjamin Amblard, Sina Tebianian. CFD Simulation for Characterization and Scale-Up of Pulsed Biomass Transport. Chemical Engineering Science, 2022, 255, pp.117652. 10.1016/j.ces.2022.117652 . hal-03705435

HAL Id: hal-03705435 https://ifp.hal.science/hal-03705435

Submitted on 27 Jun2022

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3	CFD Simulation for Characterization and
4	Scale-Up of Pulsed Biomass Transport
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ABSTRACT

Stable feeding of biomass powders into reactors represents a technical operational 13 14 challenge for renewable energy generation. The injection of sawdust powders has been recently published with a horizontal pressurized gas injector under several experimental conditions. 15 16 Valid numerical models are useful for hydrodynamic characterization of different equipment scales, such as computational fluid dynamics (CFD). In this study, the applicability of the CFD 17 multiphase particle-in-cell approach (MP-PIC) for the considered injector is investigated. The 18 model is tested under different operating conditions, showing relative deviations lower than 19 14% and 2% for solids flux and flow concentration experimental data. The effect of model 20 21 inputs (mesh refinement, drag model, particle-to-wall interaction) on the system's 22 hydrodynamics is discussed. The gas-solid flow hydrodynamics is obtained from the simulations providing additional insight on pulsed biomass transport. Ultimately, the model is 23 24 used to investigate different injector diameters and to propose a feeder operation map as a 25 function of dimensionless parameters.

Keywords: CFD, MP-PIC, Barracuda, pneumatic transport, bulk solids handling, nonmechanical feeder.

28 1 Introduction

29 Solid biomass wastes are generated in large amounts daily from industrial plants to commercial businesses such as markets and restaurants, as well as from farm crops to residential 30 sector. Instances of common biomass residues are given by sawdust, spent coffee grounds, 31 sugarcane bagasse, rice husks, poultry litter and fruit peels. Decentralized generation of wastes 32 33 is an obstacle to its reuse because collection costs often outweigh reuse profits for such inexpensive and difficult-to-handle bulk solids. On the other hand, wastes generation is 34 35 centralized in industries which allows for in-situ processing of biomass wastes into fuels or renewable energy to improve companies' energy balance and reduce their carbon footprint 36 37 (McKendry, 2002; Perea-Moreno et al., 2019).

38 Fuels and renewable energy generation is directly related to efficient injection of biomass particles into reactors producing a good penetration and mixing. This task is quite challenging 39 due to variations in samples' particle-size distribution, shape, and moisture content. Such 40 41 variations might worsen samples' flowability thus increasing its likelihood to clog feeders or result in unstable flow (Ramírez-Gómez, 2016; Ilic et al., 2018). Biomass feeding to reactors 42 might be performed under batch, semi-continuous or continuous mode using mechanical or 43 non-mechanical feeding devices with associated pros and cons (Berruti et al., 2009; Dai and 44 Grace, 2011; Dai et al., 2012; Woodruff et al., 2012; Massaro Sousa and Ferreira, 2020b, 2020a; 45 46 Bai and Si, 2021; Gomes et al., 2021).

Recently, the hydrodynamics of a horizontal pressurized injector for feeding sawdust powders (mean diameter from 447 to 1,130 μ m) into fluidized beds has been experimentally investigated with a high-speed camera (Massaro Sousa et al., 2021). The feeder showed stable and wide range of operation, with solids mass flux ranging from 60 to 450 kg/m² representing relevant conditions for solid pneumatic injection into fluidized beds. Given the available experimental data, validation of numerical models based on computational fluid dynamics and the development of scale-up rules is of great interest for advancing the state of the art for thisinjector.

The commercial software CPFD Barracuda[®] implemented the multiphase particle-in-cell 55 approach (MP-PIC) to solve motion equations for gas/particles flow, and it is gaining interest 56 particularly because samples' particle-size distribution can be fully added and the simulations 57 are solved in a time-effective way. Equipment from bench-to-industrial scale have been already 58 simulated with this software for a wide range of applications, such as FCC regenerators, 59 fluidized beds under different regimes, coal gasifiers, chemical looping combustors, pneumatic 60 conveyors, etc (Chen et al., 2013; Amblard et al., 2015; Fotovat et al., 2015; Solnordal et al., 61 62 2015; Ariyaratne et al., 2017; Chladek et al., 2018; Kraft et al., 2018; Tu and Wang, 2018; 63 Bandara et al., 2021; Pal and Theuerkauf, 2021; Sung et al., 2021).

This paper presents the simulation of the mentioned pressurized gas injector with sawdust 64 powders using the CFD MP-PIC approach implemented in the Barracuda commercial code. To 65 the best of author's knowledge, this is the first simulative study addressing this type of non-66 mechanical feeder, which deals with a fast release of pressurized gas to transport and inject 67 biomass powders into fluidized beds. First, the numerical model is compared with experimental 68 data and the effect of some model inputs on system's hydrodynamics is discussed. Finally, the 69 70 resulting model is used to extrapolate the feeder behavior at different operating and design conditions. 71

72 2 Material and Methods

73 2.1 Experimental setup and data

The system dimensions described elsewhere (Massaro Sousa et al., 2021) are shown in Fig. 1. It consists of a 0.02 m-internal diameter pipe that is divided in two sections (i.e., pressurized chamber and injection line) when the ball valve is closed. Initially, a given mass of solids (*M*) is stored at the left section that is pressurized with different gas pressures (*P*). Once the ball valve is manually opened, the solids are transported to the cold-flow unit due to gas pressure release and momentum transfer. A continuous low secondary air velocity (*U*) can be also added to minimize the accumulation of powders in the injection line.



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Fig. 1. Injection system for sawdust powders: a) experimental unit, b) geometry and mesh, c) initial and
boundary conditions, d) monitored planes: I, II, III, and IV.

The gas-solid hydrodynamics in the injection line has been investigated for different operating conditions of *P* and *M*, using a high-speed camera with acquisition rate of 3,000 images/s (Massaro Sousa et al., 2021). The experimental flow time (t_e), mean solids mass flux (G_S) and solids flow concentration (ε_S) determined previously are used here for numerical model testing. Note that t_e was measured experimentally and represents the time interval for powders to be released from the pressurized chamber and settle in the injection line. Another parameter considered in model/experiments comparison is R, which represents the mass of residual sawdust in the injection line after total gas release from the pressurized chamber divided by M.

Experimental data is shown in Table 1 for eight different injection conditions, with *P* and *M* range from 300 to 500 kPa and 0.003 to 0.024 kg, respectively. The secondary superficial gas velocity (*U*) was maintained at 4.4 m/s under all conditions. Note that V_S/V_A is the ratio of the initial volume of solids to the volume of the pressurized air at normal conditions in the chamber, as illustrated in Fig. 1a. This parameter impacts the solid concentration in the injection line:

$$\frac{V_S}{V_A} = \frac{M}{\left(V - \frac{M}{\rho_p}\right) \cdot \left(\frac{T_{ref}}{T}\right) \left(\frac{P}{P_{ref}}\right) \rho_p}$$
(1)
$$V_A = \frac{\left(V - \frac{M}{\rho_p}\right) \cdot \left(\frac{T_{ref}}{T}\right) \left(\frac{P}{P_{ref}}\right)}{V}$$
(2)

99 in which *V* is the volume of the pressurized chamber, equal to 1.73E-4 m³, whereas T_{ref} and P_{ref} 100 are 273.15 K and 101.33 kPa, respectively.

Tests	P (kPa)	M (kg)	V_{S}/V_{A} (-)	$t_{e}(\mathbf{s})$	$G_S (kg \cdot m^{-2} \cdot s^{-1})$	e _s (-)	R (%)
1	500	0.003	0.0036	0.045	210	0.058	0.3
2	400	0.003	0.0045	0.049	190	0.065	0.7
3	300	0.003	0.0060	0.096	100	0.089	3.1
4	300	0.006	0.0122	0.134	138	0.103	2.7
5	500	0.012	0.0152	0.134	284	0.113	0.9
6	400	0.012	0.0190	0.147	254	0.123	2.6
7	300	0.012	0.0253	0.167	216	0.137	5.6
8	500	0.024	0.0328	0.212	350	0.157	2.9

Table 1. Summary of the injection conditions and experimental data.

102 2.2 Injector geometry and mesh

103 The injector geometry was built in Catia V5[®] with the same dimensions of the 104 experimental feeder. The mesh was generated directly on the simulation software, Barracuda 105 Virtual Reactor[®] 21.0, mainly with cubic cells except for a few that are cut by the walls, as
106 shown in Fig. 1b. The ball valve and secondary air inlet are considered in the simulations
107 through boundary conditions as given in Fig. 1c.

A mesh refinement study was conducted in one condition (Test 5) as presented in Fig. 2. 108 The solids flux and simulation time (t^*) for different mesh refinement (N) are presented. While 109 the simulation time increases up to 23 times from coarse to fine mesh, the solids flux shows a 110 weak dependence with N, as G_S increases only about 15% in the same interval. Thus, to achieve 111 a compromise between simulation time and accuracy, 48,100 cells was selected for simulating 112 the 2-cm diameter solids injector. This compromise allows also to use similar cell sizes for the 113 114 simulation of larger injector geometries as presented later in this paper. The selected mesh corresponds to a cell density of 162 cells/cm³ considering that the total geometry volume is 115 2.97E-4 m³. 116



Fig. 2. Solids flux (G_S) and simulation time (t^*) as a function of number of cells (N). P and M are set as in test 5. **119** 2.3 Numerical model

120 The multiphase particle-in-cell (MP-PIC) method consists in using a hybrid 121 Eulerian/Lagrangian approach to solve mass and momentum balances for gas and particles, as 122 described below (Andrews and O'Rourke, 1996; Snider, 2001). The gas phase is treated as a 123 continuum in a Eulerian framework by solving the averaged Navier-Stokes equations for mass 124 and momentum:

$$\frac{\partial(\alpha_g \rho_g)}{\partial t} + \nabla \cdot \left(\alpha_g \rho_g \overrightarrow{u_g}\right) = 0 \tag{3}$$

$$\frac{\partial(\alpha_g \rho_g \overrightarrow{u_g})}{\partial t} + \nabla \cdot \left(\alpha_g \rho_g \overrightarrow{u_g} \overrightarrow{u_g}\right) = -\alpha_g \nabla P + \alpha_g \rho_g \vec{g} + \nabla \tau_g - F \tag{4}$$

in which α_g , ρ_g , $\overrightarrow{u_g}$ are the volume fraction, density, and velocity of the gas, respectively, while ∇P is the pressure gradient in the system. The gas stress tensor (τ_g) is shown in Eq. (5), while F represents the momentum exchange rate between gas and solid phase.

$$\tau_g = \mu_g \left(\nabla \, \overrightarrow{u_g} + \nabla^T \, \overrightarrow{u_g} \right) - \frac{2}{3} \mu_g \nabla \, \overrightarrow{u_g} I \tag{5}$$

Particles are treated with a hybrid Eulerian-Lagrangian approach where the mass andmomentum balances for the solid phase are given by:

$$\frac{\partial(\alpha_s \rho_s)}{\partial t} + \nabla \cdot (\alpha_s \rho_s \overrightarrow{u_s}) = 0 \tag{6}$$

$$\frac{\partial(\alpha_{s}\rho_{s}\overrightarrow{u_{s}})}{\partial t} + \nabla \cdot (\alpha_{s}\rho_{s}\overrightarrow{u_{s}}\overrightarrow{u_{s}}) + \nabla\tau_{s} + \alpha_{s}\nabla P = \alpha_{s}\rho_{s}\overrightarrow{g} + \iint fm_{p}D(\overrightarrow{u_{g}} - \overrightarrow{u_{p}})dm_{p}du_{p}$$

$$-\nabla \left[\iint fm_{p}(\overrightarrow{u_{p}} - \overrightarrow{u_{s}})(\overrightarrow{u_{p}} - \overrightarrow{u_{s}})dm_{p}du_{p}\right]$$
(7)

130 in which, the mean solid velocity $(\overrightarrow{u_s})$ and solid volume fraction (α_s) are defined by:

$$\overrightarrow{u_s} = \frac{1}{\alpha_s \rho_s} \iint f m_p \overrightarrow{u_p} \, dm_p du_p \tag{8}$$

$$\alpha_s = \iint f \frac{m_p}{\rho_s} dm_p \, du_p \tag{9}$$

$$\alpha_g + \alpha_s = 1 \tag{10}$$

In Eq. (7), f is the particle probability distribution (Snider, 2001) while D is the drag function. With the MP-PIC method, the particle probability distribution f is discretized into clouds which represent a certain number of particles with same diameter, mass, and velocity. At a given simulation time t, the cloud properties are interpolated to the Eulerian grid to solve the solid phase equations. Once the equations are solved on the grid, the Eulerian grid properties such as gas velocities, gas pressure gradients and solids stress gradients are interpolated back to the clouds to update their positions and velocity using a lagrangian approach with the following equations. The position of the cloud at the next time step x_p^{n+1} is calculated with Eq. (11) where x_p^n is the cloud position at the current time step, Δt is the time step and U_p^{n+1} is the cloud velocity at the next time step.

$$x_p^{n+1} = x_p^n + \Delta t \ U_p^{n+1} \tag{11}$$

141 Then, U_p^{n+1} is calculated as:

$$U_{p}^{n+1} = \frac{U_{p}^{n} + \Delta t \left[D U_{g,p}^{n+1} - \frac{1}{\rho_{s}} \nabla P_{p}^{n+1} + g - \frac{1}{\alpha_{s} \rho_{s}} \nabla \tau_{p}^{n+1} \right]}{1 + \Delta t D}$$
(12)

142 In which $U_{g,p}^{n+1}$ is the gas velocity at $t+\Delta t$ interpolated to the cloud position; P_p^{n+1} is the pressure 143 at $t+\Delta t$ interpolated to the cloud position; τ_p^{n+1} is the solid stress at $t+\Delta t$ interpolated to the cloud 144 position.

One of the drag models employed in this study is based on Energy-Minimization Multi-Scale (EMMS) approach, with the following expression:

$$D = \frac{9}{8} \frac{\mu_g}{\rho_p d_p^2} f_e \tag{13}$$

$$f_{e} = \begin{bmatrix} \frac{1}{18\alpha_{g}} \left(c_{0} \frac{\alpha_{s}}{\alpha_{g}} + c_{1} R e \right) & \alpha_{g} < 0.74 \\ \alpha_{g} \ge 0.74 \text{ and } R e < 1000 \\ \alpha_{g} \ge 0.74 \text{ and } R e > 1000 \\ \alpha_{$$

in which, $c_0=150$, $c_1=1.75$, $c_2=1.0$, $c_3=0.15$, $c_4=0.44$, $c_5=-0.576$, $c_6=0.0214$, $c_7=-0.7463$, $c_8=0.0044$, $c_9=-0.0101$, $c_{10}=0.0038$, $c_{11}=-0.7789$, $c_{12}=0.0040$, $c_{13}=-31.8295$, $c_{14}=32.8295$, and $c_{15}=0.687$. Note that the EMMS is already implemented in Barracuda and the values for the constants are based on a previous study (Yang et al., 2004). 151 The solid phase stress tensor (τ_s), also present in Eq. (7), is given by:

$$\tau_s = \frac{10P_s \alpha_s^{\ \beta}}{max \left[\alpha_{s,max} - \alpha_s , \ \varepsilon_p (1 - \alpha_s) \right]}$$
(16)

152 in which P_s is a constant with units of pressure (1 Pa), $\alpha_{s,max}$ is the solid volume fraction at 153 close pack, β is a constant between 2 and 5 and a value of 3 was utilized in this study, and ε_p 154 is a very small number (10⁻⁸). Comparatively, the modeling of the solid phase stress tensor is 155 simpler than the one used in the kinetic theory of granular flow where a specific equation is 156 used for the transport of the granular temperature (Lun et al., 1984; Gidaspow, 1994).

157 The colisions of the solid phase with walls are considered with Eq. (17). The resulting 158 particles cloud velocity $(\overrightarrow{u_p})$ following a wall impact, at the instant n+1, is decreased by normal 159 (η_n) and tangential (η_t) retention parameters for momentum losses and angle of impact with 160 respect to the vertical direction (θ) :

$$\overline{u_p}^{n+1} = \left[(\eta_n - \eta_t)(1 - \cos\theta) + \eta_n \right] \overline{u_p}^n \tag{17}$$

161 2.4 Simulation conditions

The solid injection simulations were performed under the conditions shown in Table 1. Simulations were performed in Barracuda Virtual Reactor[®] 21.0 with a Linux computer (Intel[®] Xeon[®], E5-1620 v3, 3.5 GHz) during a total simulation time of 0.3s, and with a time step of 10^{-5} s. Simulating 0.3s is sufficient to cover all experimental conditions because the maximum experimental flow time is 0.212s (test 8).

167 The initial and boundary conditions are depicted in Fig. 1c. A given mass of sawdust 168 powders (M) is initially packed in the solids injector, at the same location as experimentally, 169 while the gas phase is pressurized at a given P in the chamber region. The pressure on the 170 injection line and ball valve regions are set as 100 kPa (atmospheric pressure), and outflow for 171 gas and solids is set at the boundary of the cold-flow unit also with 100 kPa. A secondary air 172 velocity (U) of 4.4 m/s is added perpendicularly to the injection line through a square plane of equal area than the experimental inlet. Finally, a wall boundary condition is set on the left endof the pressurized chamber.

Some planes were created in the geometry to monitor the gas-solid flow, as shown in Fig. 176 1d, such as planes I, II, III, and IV. Flow data was acquired every 10⁻⁴s to fully capture the gas-177 solid hydrodynamics in the injection line, which physically corresponds to a fast transport of 178 bulk solids by pressurized gas release. Note that the region between planes II and III 179 corresponds to the same location that the gas-solid flow was assessed experimentally with the 180 high-speed camera (Massaro Sousa et al., 2021).

In the simulations, mean values for G_S and ε_s were obtained considering the positions and experimental data acquisition methods (Massaro Sousa et al., 2021). Thus, the solids mass flux passing through plane III was monitored and integrated until 99.5% of the cumulative mass curve is reached ($M_{99.5\%}$). The corresponding flow time $t_{99.5\%}$ provides the G_S as:

$$G_S = \left(\frac{M_{99.5\%}}{A.\,t_{99.5\%}}\right) \tag{18}$$

in which *A* is the cross-sectional area of the injection line of 3.14E-4 m². The mean solids fraction is obtained iteratively by Eq. (19), which is the same equation used to average the experimental results. Note that ε_s calculated from Eq. (19) is a volumetric ratio which agrees with the solids fraction definition:

$$\varepsilon_S = \frac{Q_S}{Q_t + Q_S} = \frac{\frac{G_S A}{\rho_p \varepsilon_s}}{Q_t + \frac{G_S A}{\rho_p \varepsilon_s}}$$
(19)

in which Q_t is the volumetric gas flowrate in plane III averaged until $t_{99.5\%}$. We have also verified that using Eq. (19) is consistent with the cross-sectional mass-weighted average ε_S gathered from the simulations. Finally, *R* is calculated by dividing the mass of solids accumulated in the injection line at the end of simulation by *M*.

193 The drag model used was based on the Energy-Minimization Multi-Scale (EMMS), and 194 the normal (η_n) and tangent-to-wall (η_t) parameters were set as 0.70. A detailed study about these parameters is presented in Sections 3.1 and 3.2, respectively. Other variables have been maintained as Barracuda's default, such as: close pack volume fraction of 0.60, diffuse bounce of 5, and particle-particle interactions ($P_s=1$ Pa, $\beta=3$, $\varepsilon_p=10^{-8}$, m=40%).

198 2.5 Sawdust properties

The particle size distribution of the sawdust sample is shown in Fig. 3 with d_{50} of 647 199 µm. The cumulative curve has been fully inserted in the simulations along with the particle 200 density of 1,030 kg/m³ (Geldart B), and initial particle volume fraction of 0.21 (averaged 201 between loose and tapped conditions). Note that the particle volume fraction of sawdust is 202 203 within the range of typical values for other biomass particles, generally from 0.07 to 0.30, as reported in the literature (Tannous et al., 2013; Dhiman et al., 2016; Massaro Sousa and 204 Ferreira, 2019). The methods for sample characterization are presented in detail elsewhere 205 206 (Massaro Sousa et al., 2021). The particle shape factor was considered as 1 in the simulations.





- 209 3 Results and Discussion
- 210 3.1 Effect of the drag model

In the following sections, the influence of the drag model and particle-to-wall interactionsare investigated to find the best set that represents the experiments. To minimize the number of

simulations, the parameters' effect were studied under operational settings of test 5 (Table 2),
however similar effects are expected under conditons of tests 1-8.

Different drag models have been evaluated to predict the horizontal transport of sawdust from the injector, consisting of Gidaspow (GD), Turton-Levenspiel (TL), Haider-Levenspiel (HL), and Energy-Minimization Multi-Scale (EMMS). These drag models are already implemented in Barracuda Virtual Reactor[®] 21.0 and commonly used for gas-solid flows (Turton and Levenspiel, 1986; Haider and Levenspiel, 1989; Gidaspow, 1994; Yang et al., 2004; Chen et al., 2013).

In Fig. 4, simulation results for solids mass flux matches experimental data (white bar) 221 222 accurately with the EMMS drag model, whereas the other homogeneous drag models overestimated the solids flux by 6 to 9 times. Thus, the EMMS has been selected for the 223 simulations of this work. Previous MP-PIC studies have also demonstrated improved 224 hydrodynamics predictions with the EMMS method, while overstimation of fluidization 225 patterns were observed with the other drag models for circulating fluidized beds with Geldart 226 B and D (Kraft et al., 2017; Kraft et al., 2018; Tu and Wang, 2018) and fluidized beds with 227 Geldart A (Feng et al., 2018). A recent MP-PIC study on pneumatic conveying of drill cuttings 228 $(d_{50}=290 \,\mu\text{m}, \rho_p=2.715 \,\text{kg/m}^3, \text{Geldart B})$ used the Gidaspow drag model multiplied by 0.50 to 229 230 reduce the drag force and match the pressure drop and particle velocity in their pipeline (Sung et al., 2021). 231



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233 Fig. 4. Solids flux (G_S) for various drag models with P and M set as in test 5.

234 3.2 Effect of particle-to-wall collision

Particle-to-wall interactions are adressed in Barracuda® with two main parameters, 235 accounting for normal (η_n) and tangent (η_t) collisions with the wall. A value of 1.0 indicates a 236 perfectly elastic collision, which means that the particle bounce back from or slide tangent to 237 the wall with the same momentum before the contact, whereas 0.0 indicates that the momentum 238 is entirely dissipated. Information about such parameters are difficult to be obtained 239 experimentally, thus different values have been numerically investigated from 0.85 to 0.10, and 240 its effect on the injector dynamics are presented in Fig. 5. Since both parameters are unknown, 241 242 we used the same values for η_n and η_t while analysing their effect on the responses.

243 The cumulative mass of sawdust passing through plane III (M^*) is shown in Fig. 5a during 0.3s of simulation for different η_n and η_t . The shape of the curves are similar among each other, 244 with an initial fast transport of solids followed by an asymptotical pattern due to the decrease 245 246 of the pressurized chamber gas, which is the driving force for the transport of solids. Besides, curves become less inclined as parameters values decreases to 0.10, indicating that the mean 247 solids mass flux decreases by decreasing η_n and η_t . For example, G_S decrease by 11% from 0.85 248 to 0.10. Moreover, as shown in Fig. 5b, there is a significative increase in the accumulation of 249 sawdust in the injection line (R), from 0.2 to 12.3%, by decreasing η_n and η_t from 0.85 to 0.10 250 which is due to higher friction among the particles and wall. 251

These results are in agreement with the expected behavior, since enhanced loss of momentum occurs with lower parameters values, hence decreasing G_s and increasing R. For the simulation of the solids injector with sawdust, η_n and η_t have been fixed at 0.70 to match experimental data for test 5 (R and G_s). Note that 0.70 is within the range of recommended values in Barracuda's manual, as typical parameters values of 0.50 and 0.85 are used for soft and hard particles, respectively.



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Fig. 5. Simulated results for different η_n and η_i : a) sawdust mass passing through plane III (*M**), and b) accumulation of powders in the injection line (*R*). *P* and *M* are set as in test 5.

262 3.3 Numerical model testing

In this section, the numerical model is tested under different operating conditions, tests 1 to 8 (Table 1). A consistent quantitative agreement between simulated and experimental data is presented in Fig. 6, in terms of solids mass flux, flow time, and flow concentration. On average, relative deviations were lower than 14, 11, and 2% for G_S , ε , and t_e , respectively, from tests 1 to 8 (0.0036 $\leq V_S/V_A \leq$ 0.0328). The relative deviations were calculated as the difference between simulated and experimental values divided by the experimental one.

As demonstrated experimentally (Massaro Sousa et al., 2021), depending on the initial settings for *M* and *P*, different solids mass flux and flow concentrations can be obtained in the injection line. The numerical model accurately reproduced such behaviors from tests 1-8. Under stable operating conditions, higher solids mass fluxes are obtained by using higher gas pressure and/or initial mass of solids in the injector. Fig. 6a presents the trends of simulation data under decreasing *P* (points 1 to 3, and 5 to 7) or increasing *M* (points 3 to 4, and 7 to 8) for different V_S/V_A values. The qualitative experimental behavior was reproduced extremely well by the simulations, specially for $0.005 \le V_S/V_A \le 0.020$ with relative deviations of 5% (within the experimental error bars). Outside of this range, the deviations reached up to 20%, possibily because the pulse injections were either more dilute or dense compared to the conditions of test 5 (V_S/V_A =0.0152), which was used for selecting the drag model and particle-wall parameters.

Moreover, it was observed experimentally that both flow time and solids concentration in the injection line increase as V_S/V_A increases (i.e., with increasing initial solids ratio in the injector), and the numerical model also predicts it as presented in Figs. 6b and 6c.



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The transient behavior for the injection of sawdust powders is illustrated in Fig. 7 under test 5 conditions. The discrete phase is coloured according to the particle velocity, from 0 to 80 m/s, while the continuous phase is painted in terms of gas pressure, from 100 to 500 kPa, as it is the driving force for the solids transport. At *t*=0s, the particles are at rest and the gas is pressurized in the chamber with P=500 kPa.

As soon as the simulation starts, the gas is released downstream with P dropping rapidly 294 to 400, 300, and 200 kPa in 0.009s, as shown in Figs. 7b to 7d, respectively. In this interval, the 295 296 solids are accelerated by transfer of gas momentum, and there is a distribution of particle velocities and concentrations along the geometry. At the injection line section, there is initially 297 a dilute transport of solids at high-speed (Fig. 7b), followed by a more dense flow with velocity 298 from 30 to 80 m/s (Figs. 7c to 7d). On the other hand, at the pressurized chamber region the 299 solids velocity are generally lower than 30 m/s. These features are in line with experimental 300 301 observations with a high-speed camera at 3,000 frames per second (Massaro Sousa et al., 2021).





Fig. 7. Countors for particles velocity (discrete phase colour) and gas pressure (background colour) at different times. *P* and *M* are set as in test 5.

In the images, the coloring scale range has been reduced to better assess the phenomena. 305 From Fig. 7e and onwards, a decelerating flow of solids is verified due to a combined effect of 306 pressurized gas emptying at the solids injector chamber ($P \approx 100 \text{ kPa}$) and loss of momentum by 307 particle-particle and particle-wall collision. The solids are homogeneously distributed along 308 injection's line diameter, until they begin to settle at the lower section of the tube (Fig. 7m), 309 and their residual movement is due to the powder's inertia and bouncing. Finally, there is almost 310 no transport of powders at t=0.3s, and the residual solids accumulate throughout the base of the 311 injection line (Fig. 7p). 312

The transient behavior can be also visualized in Fig. 8, in which the flow concentration (ε_S) and total interstitial gas velocity (U_t) were averaged in the cross-sectional plane III over time, while the gas pressure was averaged in plane I (Fig. 1d). As previously described, there is a fast decrease in *P* due to gas release with ball valve opening, resulting in the transport of solids with peak values for ε_S up to 0.16, for total gas velocity up to 200 m/s, and for mean cross-sectional solids velocity up to 45 m/s. As *P* reachs atmospheric conditions, there is a deceleration pattern for ε_S , U_t and U_S until the remaining solids settle at the injection line.



Fig. 8. Flow concentration (ε_s) total interstitial gas velocity (U_i), cross-sectional solids velocity (U_s) and pressure (P) over time for conditions of test 5.

323 3.5 Model extrapolation: feeder operation map

It is interesting to investigate model's responses outside of the interval that has been tested against experimental data, particularly for operating conditions that are difficult or dangerous to be implemented experimentally. Therefore, higher gas pressures are analyzed here up to 1,650 kPa, which represents a 3.3-fold increase compared to the maximum one used in the experiments (P=500 kPa) (Massaro Sousa et al., 2021). The injector dimensions were maintained as shown in Fig. 1a, which means that, at maximum, 0.0364 kg of sawdust can be inserted into the pressurized chamber region. The simulations were performed under three solids loading conditions, V_S/V_A of 0.015, 0.025, and 0.035. The solids mass flux is shown in Fig. 9a as a function of the gas pressure. The trend of the curves are similar, with an initial linear increase of G_S as P increases, until it reachs a maximum value, followed by a decreasing trend for G_S . For example, with the solids loading of 0.015, G_S can be adjusted from 100 to 650 kg/m²s by increasing P up to 1,650 kPa.

In Fig. 9b, G_S is plotted as a function of V_A that is a dimensionless parameter related to the amount of pressurized air representing the driving force for the solids transport with this injector. The curves behavior are similar to the ones described in Fig. 9a, however with the advantage that the dimensionsless parameters (V_A and V_S/V_A) are dissociated from specific experimental conditions resulting in a more general description of the phenomena. Note that these parameters can be easily calculated before any injection of solids (i.e., from initial *P* and *M* conditions) with Eqs (1) and (2).

To explain the maximum of G_s in the curves, three points have been highlighted in Fig. 343 9b and are illustrated in Fig. 9d. These points are under the same V_S/V_A ratio with increasing 344 V_A , hence more solids are present in the pressurized chamber from points (1) to (3). As also, 345 observed experimentally, a large amount of solids in the pressurized chamber provides a 346 significant length that requires higher amount of gas for solids transport compared to when a 347 348 smaller portion of the chamber is occupied. However, as shown in Fig. 9d, this additional gas is limited because the pressurized chamber length is fixed, then there is a decrease in G_S as the 349 chamber approaches its maximum powder filling limit. 350

The phenomena described in the previous paragraph, results that, if there is not a significant amount of pressurized gas available on the left side of the packed bed (in the pressurized chamber) to push the powders ensemble, then the feeders performance is jeopardized, which means that there is a decrease in G_S and significative accumulation of solids in the injection line (e.g., R>10%) (Massaro Sousa et al., 2021). There is a dimensionless parameter, V_A^* , that captures the portion of air pressurized on the left side of the packed bed, as illustrated in Fig. 9d. It is calculated by considering the mean bulk density between loose and tapped conditions (ρ_m of 215 kg/m³):

$$V_A^* = \frac{\left(V - \frac{M}{\rho_m}\right) \cdot \left(\frac{T_{ref}}{T}\right) \left(\frac{P}{P_{ref}}\right)}{V}$$
(20)

Experimentally the feeder malfunction occured for $V_A^* \le 1.4$, thus the simulations were performed here considering $V_A^*=1.6$ as the operating limit. The G_S curve plotted as a function of V_A^* is presented in Fig. 9c for the studied V_S/V_A , showing the curve inversion pattern (maximum G_S point) as a consequence of increasing solids loading in the injector.

Another remark on the operation map (Fig. 9c) is that for a given V_A , the higher the initial solids inventory (V_S/V_A) the higher G_S because the injection of sawdust occurs in a more dense condition as was the case experimentally. This is highlighted in Fig. 9e by the mean flow concentration from 0.12 to 0.20, in the interval of $0.015 \le V_S/V_A \le 0.035$. Ultimately, Figs. 9b and 9e are useful for estimating G_S and ε_S for the actual injector by interpolating the curves, which are valid for a broad range of conditions (i.e., $0.015 \le V_S/V_A \le 0.035$, and $1.8 \le V_A \le 12.7$, with the restritive condition that $V_A * \ge 1.6$), at least according to the simulations.



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Fig. 9. Solids mass flux as a function of a) *P*, b) V_A , and c) V_A *, as well as d) initial settings for marked points (1) to (3) with V_S/V_A =0.015 and e) solids flow concentration versus V_A .

378 3.6 Model extrapolation: effect of the injector diameter

379 In this section, the numerical model is used to simulate injectors with larger internal diameters aiming at evaluating feeders for larger scale applications in a cost-effective way. 380 Three different operating conditions were tested to cover dilute to dense injections, with V_S/V_A 381 of 0.0036 (test 1), 0.0152 (test 5), and 0.0328 (test 8). The simulation setup and the cell size is 382 equal to that validated in Section 3.3, however the initial condition for solids and gas were 383 384 adjusted to match the same V_S/V_A ratio since the injector volume increases with increasing D. Thus, the gas pressure in the pressurized chamber was maintained at 500 kPa, equal to tests 1, 385 5, and 8 (Table 1), whereas the initial mass of solids was increased to meet similar V_S/V_A . It 386 387 means that batch injections of sawdust were performed from 0.003 to 0.890 kg.

The results for mean solids flux and flow concentration are presented in Fig. 10a and 10b, respectively, for diameters from 0.02 to 0.12 m, with the latter representing a 6-fold increase of this parameter. Similar values for G_S and ε_S are observed in the range of $0.02 \le D_I \le 0.12$ m, for all different initial conditions of V_S/V_A . It indicates, at least according to these simulations, that wall effects are not predominant to jeopardize the performance of this injector for $D_I \ge 0.02$ m, providing an important conclusion for developing scale-up and operation rules for this solids injector. Ultimately, the operation map shown previously (Fig 9b and 9c) might also be employed for estimating G_s for injectors with $D_i \ge 0.02$ m.



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In Fig. 10c, the simulation time (t^*) and number of cells are presented for different D_I and V_S/V_A. There is an exponential increase in t^* with increasing D_I because the mesh cells in the geometry also increases exponentially. The same mesh density of 162 cells/cm³ (i.e., same cells size) has been used in the simulations to prevent mesh-related uncertanties in the calculations. 405 Moreover, for implementation purposes, it is important to highlight that simulations with 406 greater initial quantity of solids (i.e., those with higher V_S/V_A) demand more time to be finished 407 with the Barracuda software because of the higher number of clouds to track. For example, in 408 our case, the simulations with V_S/V_A of 0.0328 takes from 2.5 to 4.8 times more time to finish 409 than those with V_S/V_A of 0.0036.

410 **4** Conclusions

In this study, the applicability of a commercial CFD code with the MP-PIC approach is 411 demonstrated to simulate the transport of biomass with a pressurized gas feeder. After testing 412 413 against experimental data, the numerical model is used to simulate various operation conditions (P and M), and to study the system transient hydrodynamics. The model is then extrapolated, 414 and an operation map is build-up for the injector as a function of dimensionless parameters 415 related to the initial solids loading and driving force intensity (V_S/V_A and V_A). The model is also 416 417 extrapolated to study the influence of the injector diameter (D_I) which is a key parameter for 418 injector's scale-up.

419 The experimental results were accurately reproduced after some investigations on the drag law and particle-to-wall parameters. The drag law was more important to tune G_S while 420 421 the particle-wall interactions affected the accumulation of powders in the injection line (R). The solid-stress tensor function used in Barracuda, Eq. (16), is notably simpler than the set of 422 equations employed by the kinetic theory of granular flow. Thus, careful analysis should be 423 performed to assess the suitability of Eq. (16) to different applications, particularly for dense 424 425 systems. The nature of the multiphase flow analyzed here, consisting of a dilute batch flow of 426 solids ($\varepsilon_{\rm S}$ <0.20) may have contributed to some extent to the good model predictions.

In terms of the simulation results, the model has been extrapolated to different conditions of gas pressures and injector diameters in Sections 3.5 and 3.6. An assessment of the deviations of these predictions should be performed in the future with the availability of experimental data. Future studies could simulate this solids injector with powders of different properties (particle density and size distribution) to cover other applications. Besides, further investigations could focus on validating the model for predicting gas-solid jet penetration in fixed and fluidized beds with this injector.

434 5 Nomenclature

A	Cross-sectional area of the injection line (m^2)
$c_0 to c_{15}$	Drag function constants (-)
D	Drag function (-)
D_I	Injector diameter (m)
d_p	Particle diameter (m)
d_{10}	Volumetric diameter for 10% of samples' particle-size (µm)
d_{50}	Volumetric diameter for 50% of samples' particle-size (µm)
d_{90}	Volumetric diameter for 90% of samples' particle-size (µm)
F	Gas-solid momentum exchange rate (kPa)
f	Particle probability distribution
fe	Drag function parameter (-)
\vec{g}	Gravity aceleration $(m \cdot s^{-2})$
G_S	Solids mass flux $(kg \cdot m^{-2} \cdot s^{-1})$
Ι	Unit tensor (-)
М	Initial mass of sawdust in the injector (kg)
M99.5%	Mass of sawdust at 99.5% of the cumulative curve in plane III (kg)
M^*	Cumulative mass of sawdust passing through plane III (kg)
М	Maximum momentum redirection from collisions (%)
m_p	Mass of a particle cloud (kg)
Ν	Number of mesh cells (-)
Р	Air pressure in the injector (kPa)
Pref	Reference air pressure (kPa)
P_s	Constant in Eq. (16) (kPa)
P_p^{n+1}	Pressure interpolated to cloud position at instant $n+1$ (kPa)
Q_{s}	Volumetric solid flowrate (m ³)
\tilde{Q}_t	Volumetric total gas flowrate (m^3)
Ŕ	Mass of sawdust accumulated on the injection line (%)
Re	Reynolds number (-)
Т	Time (s)
te	Experimental injection flow time (s)
t^*	Simulation time (h)
$t_{99.5\%}$	Simulated injection flow time (s)
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T_{ref}	Reference air temperature (K)
$\overrightarrow{u_{q}}$	Gas phase velocity vector $(m \cdot s^{-1})$
$U_{a,p}^{n+1}$	Gas velocity interpolated to cloud position at instant $n+1$ (m·s ⁻¹)
$\overrightarrow{u_n}$	Particle cloud velocity vector $(m \cdot s^{-1})$
$\frac{p}{u_n}n$	Particle cloud velocity vector at instant n ($m \cdot s^{-1}$)
$\overrightarrow{u_n}^{p}^{n+1}$	Particle cloud velocity vector at instant $n+1$ (m·s ⁻¹)
U_n^{n+1}	
$\overrightarrow{u_c}$	Solid phase velocity vector $(m \cdot s^{-1})$
U	Secondary air velocity $(m \cdot s^{-1})$
U_t	Total air velocity ($m s^{-1}$)
Us	Cross-sectional solids velocity $(m \cdot s^{-1})$
V	Volume of the pressurized chamber (m^3)
VA	Initial volume of air defined in Eq. (2) (-)
V_A^*	Initial volume of air defined in Eq. (20) (-)
V_{S}/V_{A}	Volume of solids divided by volume of air as in Eq. (1) (-)
x_n^n	Cloud position at instant $n(m)$
x_n^{n+1}	Cloud position at instant $n+1$ (m)
···p	r · · · · · · · · · · · · · · · · · · ·
Greek letter	
α_{g}	Gas phase fraction (-)
α_s	Solid phase fraction (-)
$\alpha_{s,max}$	Parameter in Eq. (16) (-)
β	Parameter in Eq. (16) (-)
∇P	Pressure gradient in the system (kPa)
Δt	Simulation time step (s)
η_n	Normal particle-to-wall retention parameter (-)
η_t	Tangent particle-to-wall retention parameter (-)
8	Mean air fraction in the flow (-)
ES	Mean solid fraction in the flow (-)
\mathcal{E}_p	Parameter in Eq. (16) (-)
μ_a	Gas viscosity (kg·m ⁻¹ ·s ⁻¹)
ω	Drag function parameter (-)
ρ_a	Air density $(kg \cdot m^{-3})$
ρ_m	Mean bulk density (kg·m ⁻³)
ρ_p	Particle density (kg·m ⁻³)
$\rho_{\rm s}$	Solid phase density (kg·m ⁻³)
θ	Angle of impact particle-to-wall (°)
$ au_a$	Gas phase stress tensor (kPa)
$ au_n^{n+1}$	Solid stress interpolated to instant $n+1$ (kPa)
$ au_s$	Solid phase stress tensor (kPa)

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