

# **Reference Density Database for 20 Aqueous Alkali Halide Solutions**

Fufang Yang, Jingang Qu, Georgios Kontogeorgis, Jean-Charles de Hemptinne

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<span id="page-2-0"></span> accurate density data provides insights into the structural information of the aqueous electrolyte 58 solutions .

 In aqueous electrolyte solutions, density is very different from in pure water, being up to 100% larger at high salt composition compared to pure water density at the same temperature and pressure, especially for the heavier salts. In addition, in equations of state, the volumetric parameters are more sensitive to density than to phase equilibria and thermal properties. One 63 should expect large deviations when the density is not included in the objective function  $4.5$ . Therefore, density is an important property that has to be critically evaluated before it can be used in model development.

 Obtaining a reference database for aqueous alkali halide solutions is important for many reasons. For instance:

 - While density has been extensively measured for some of the aqueous solutions, the measurements are not of the same quality. Critical evaluation of experimental data and removal of data of poor quality are essential steps.

 - The aqueous alkali halide solutions are the first systems that model developers often work on. From the perspective of model development, a reference density database is practical.

 - Many more complicated industrially relevant mixtures consist of water and one or more alkali halides. In the measured data series, usually a few data points are available for aqueous alkali halide solutions. Comparison of the aqueous alkali halide data against a reference database for the system can verify the validity of measurements of the more complicated mixtures before the data are used in industrial applications.

 In this work, density data of 20 aqueous alkali halide solutions are extensively collected and critically evaluated. Because datasets from hundreds of references are available with very different quality, a fast evaluation approach is proposed here, utilizing the support vector regression (SVR) algorithm to compare the experimental datasets against each other. Datasets that are not consistent with most other datasets are identified and removed. A reference database for the density of aqueous alkali halide solutions is proposed. Based on this reference database, correlations are developed and provided. This work, along with the databases for other properties that were 85 published previously  $6,7$ , can be used for benchmarking future developments of electrolyte equation of state. In addition to this ready-for-use state-of-the-art density database, the proposed data evaluation procedure for density can potentially be used for other properties that do not change drastically in the aqueous phase.

#### <span id="page-4-0"></span>**2 Methodology**

 In this section, the density data collection, evaluation, and correlation procedures are presented. In addition, approaches for assessing the data distribution and model applicability domain are also introduced.

#### <span id="page-4-1"></span>**2.1 Experimental density data collections**

 For the 20 aqueous alkali halide solutions, 14315 density data points of 819 datasets are 95 collected from the CERE aqueous electrolyte databank and DETHERM  $9$ . Krumgalz et al.  $10$  presented an evaluated database for densities of a few aqueous electrolyte solutions. 4 of the 20 aqueous alkali halide solutions investigated here were covered by their database. Datasets from their database have also been collected along with those from the databanks.

 In the literature, salt composition was reported in various units. Here the experimental data are converted to the same units for comparisons. Using the equations listed in Table 1, concentration units are converted to ion-based molar fraction, which is usually used in equations of state and activity coefficient models. When the pure water density is needed for the conversion from density difference or apparent molar volume, the reported value from the same reference is used. When pure water density is not provided from the experimental references, it is calculated 105 using IAPWS-95  $^{11,12}$ . In the cases that pressure was not in reported in the experimental references, it is recorded as 101.325 kPa in this database.

107 Table 1. Equations for converting concentration units to ion-based molar fraction.

	Original salt concentration unit Conversion to ion-based molar fraction <sup>a</sup>
molality	$x_i = Z_i x_i^0 / (Z x_i^0 + 1 / M_{water})$
weight fraction	$x_i = Z_i x_i^0 / M_{\text{salt}} / [Z x_i^0 / M_{\text{salt}} + (1 - x_i^0) / M_{\text{water}}]$
salt-based molar fraction	$x_i = Z_i x_i^0 / [1 + (Z_i - 1) x_i^0]$
molarity	$x_i = Z_i x_i^0/[Z x_i^0 + (\rho/1000 - x_i^0 M_{\text{salt}})/M_{\text{water}}]$
kg salt per kg solvent	$x_i = Z_i x_i^0 / M_{\text{salt}} / (Z x_i^0 / M_{\text{salt}} + 1 / M_{\text{water}})$
mol water per mol salt	$x_i = Z_i/(Z + x_i^0)$
g of salt per $100 \text{ cm}^3$ solution	$x_i = 10Z_i x_i^0/M_{\rm salt}/[10Z x_i^0/M_{\rm salt} + (\rho - 10x_i^0)/M_{\rm water}]$

108 a)  $x_i^0$  is the original salt composition unit as noted in the first column of the table.  $x_i$  is the ion-based

109 molar fraction. *Z* is the total number of ions in the salt, and is 2 for alkali halides.  $Z_i$  is the number of ions

110 *i* in the salt, and is 1 for alkali halides. *M* is the molar mass in kg/mol, taken from the NIST Chemistry

111 WebBook <sup>13</sup>.  $M_{\text{water}} = 0.0180153 \text{ kg/mol}$ .  $\rho$  is the density of the solution in kg/m<sup>3</sup>.

#### <span id="page-5-0"></span>112 **2.2 Data evaluation**

 The goal of this work is to remove datasets that are outliers, i.e., anomalies, in the collected databank. Common anomaly detection algorithms include isolation forest, robust covariance, 115 support vector regression one-class, etc  $14-17$ . These classification-based algorithms detect anomalies based on data distribution. Both response (density) and variables (temperature, composition, and pressure) are used as inputs for evaluating data distribution. However, in the scenario of this work, only the data of high accuracy can be selected in the reference database, while the algorithms are not capable of automatically distinguishing the data points that deviate from the consistent datasets by only a few percent. More importantly, in these algorithms, the scarceness of data at high temperature and pressure outweighs the deviations in density, and would result in undesirable removal of the valuable data in the scarcer region. Therefore, selection of the reference database can only be achieved based on observation of the deviations of the data points from a preliminary model that is trained to the data, which reflects deviations of the data points from each other.

 The support vector regression (SVR) is used for correlating the collected data and for comparing the data with each other. Through the Gibbs phase rule, it is known that a homogeneous mixture of water and a salt has 3 degrees of freedom, i.e., composition (*x*), temperature (*T*), and pressure (*p*). This is different from in the usual applications of the machine learning models on  predicting thermodynamic properties (e.g., group contribution and quantitative structure-property 131 relationship models (OSPR)  $18-20$ , in which case dominant features have to be selected and do not contain complete information of the response. Therefore, given datasets that are consistent with each other, the experimental data should be regressed to the SVR model with very high accuracy. The accuracy indicates agreement between the experimental datasets in addition to agreement of the datasets with the trained model. On the other hand, when a dataset deviates much from the trained SVR model in a region where other experimental datasets agree well with the model, we can conclude that the deviating dataset is inconsistent with the other experimental datasets. Plotted against the 3 degrees of freedom, it can be observed whether a data point is "deviating" beyond the scattering of other data; it can also be observed whether the data range is severely compromised when a dataset is removed as deviations are observed to be larger compared to the other datasets. When a data point from a dataset is considered to be deviating too much from the other data, the entire dataset that contains the deviating data point is removed. The procedure is repeated until all datasets agree well with each other up to a desirable accuracy without the need to remove any more experimental datasets. In general, no more than 4 regressions were needed. In the evaluation, all the data are included for regressing the SVR model, because the regressed model is intended only for comparing the datasets against each other, rather than for calculations. After the reference database is finalized, it is split into training, validation, and test sets for correlating SVR models that are used for calculations, as will be explained in Section 2.4. Figure 1 summarizes the procedure of density data evaluation and correlation. The evaluation procedure is applied for the 20 aqueous alkali halide solutions. Then, the reference database is finalized, and is used for training the SVR models.



Figure 1. Density data evaluation and correlation: (a) workflow and (b) schematics.

 Figure 2 shows a comparison of the collected data and selected data (reference database) of the (water + KCl) density as an example of the evaluation procedure. At the start, input data include some datasets that deviate from others by more than 10%, and some datasets that already deviate 157 from others by only  $1 \sim 3\%$ , but fall in the range that other datasets agree very well with each other. As these datasets are removed, agreement between the remaining datasets is improved. For this case, the procedure took 3 rounds of evaluations. The data that have been excluded in the final reference database are marked as grey in the graphs of the collected data to show the comparably larger deviations compared to the data that have been kept. In the graphs on the second row, only the kept data are shown, with a much smaller scale of deviation. Before the evaluation, the collected data present deviations of more than 15% in some cases, and much scattering in regions with a lot of data. At the end, all the remaining data agree with each other within 0.5%. The procedure is performed on the density data of the 20 aqueous alkali halide solutions.



167 Figure 2. Comparison of collected data (before evaluation) and selected data (after evaluation) of (water + 168 KCl) density. Data that are removed in the finalized reference database are marked as grey in the graphs 169 of the collected data.

### <span id="page-8-0"></span>170 **2.3 Gaussian mixture model analysis**

 The Gaussian mixture model (GMM) is a probability model that implements iterative 172 expectation maximization algorithm for analyzing data clustering  $21$ . In this work, it is used for providing a qualitative visualization of data distribution. GMMs are trained for the selected density data of each aqueous alkali halide solution. The GMM is defined as:

$$
q(\mathbf{z}|\boldsymbol{\pi}, \boldsymbol{\mu}, \boldsymbol{\Sigma}) = \sum_{k=1}^{K} \pi_k \mathcal{N}(\mathbf{z}|\mu_k, \Sigma_k)
$$
 (1)

$$
\sum_{k=1}^{K} \pi_k = 1\tag{2}
$$

175 where  $q$  is the likelihood (usually denoted as  $p$ , but noted as  $q$  here to avoid confusion with the

- 176 pressure),  $\mathbf{z} = (T, p, x)$  is the input (each data point),  $\boldsymbol{\pi} = \{\pi_1, ..., \pi_K\}$  are mixing coefficients, and
- 177  $\mu = {\mu_1, ..., \mu_K}$  and  $\Sigma = {\Sigma_1, ..., \Sigma_K}$  specify the mean and covariance of each Gaussian
- 178 component  $\mathcal{N}(z|\mu_k, \Sigma_k)$ , respectively, *k* denotes the *k*th GMM component, *K* denotes the total

179 number of GMM components, and N denotes the Gaussian distribution.  $\pi$ ,  $\mu$ , and  $\Sigma$  are 180 parameters that are trained in the GMM to approximate the data distribution,  $\boldsymbol{z}$ . Given a training 181 set, the parameters  $\pi$ ,  $\mu$  and  $\Sigma$  are first initialized via the k-means++ algorithm <sup>22</sup> and then 182 estimated through the iterative Expectation-Maximization (EM) algorithm to maximize the 183 likelihood  $^{23}$ , according to:

$$
\ln q(\mathbf{Z}|\boldsymbol{\pi}, \boldsymbol{\mu}, \boldsymbol{\Sigma}) = \sum_{n=1}^{N} \ln \sum_{k=1}^{K} \pi_k \mathcal{N}(\mathbf{z}_n | \mu_k, \Sigma_k)
$$
(3)

184 where  $\mathbf{Z} = (\mathbf{T}, \mathbf{p}, \mathbf{x})$  is the input matrix, N is the number of data points, and  $\mathbf{z}_n$  is for the *n*th data 185 point. In addition, to avoid overfitting,  $K$  is selected to minimize Bayesian information criterion 186 (BIC) <sup>24</sup>, which is defined as BIC=  $ln(N) M - 2 ln(\hat{L})$ , where N is the number of data points, M 187 represents the number of estimated parameters, and  $\hat{L}$  denotes the maximized value of the 188 likelihood function of the model.

 GMM can provide a qualitative visualization of data distribution using a contour plot. In addition, its convergence also reflects to some extent the quality of our collected database. Furthermore, in this work, we also use the GMM to determine if calculated data points can be 192 regarded as within the range of the database. The procedure is known as novelty detection  $25$ . Any data point located in a low data-distribution-density region can be considered a novelty. In this way, GMM enables us to determine whether our database can be applied to a new condition. An executable program is provided in the Supplementary Material for calculations. The GMM plot of the database is presented in the user interface as calculations are made. In this way, whether the calculations are within the ranges of the proposed database is visualized.

#### <span id="page-9-0"></span>198 **2.4 Support vector regression (SVR)**

SVR provides the flexibility to define how much error is acceptable in the regression  $26$ . Deviations below a threshold, *ε*, are considered unimportant. In this way, a tube is defined of which the centerline is the prediction of the SVR model. Within the tube, deviations are not penalized in the objective function. The very idea of SVR is suitable for identifying datasets that present larger deviations compared to others. Advantages of SVR include that its generalization capability and 204 prediction accuracy are excellent  $27$ . Therefore, SVR is very suitable for evaluating and correlating

- 205 data of thermodynamic properties, for which extensive measurements are prohibitively expensive,
- 206 and evenly distributed data are usually unavailable.
- 207 In SVR, Eq. (5) is minimized subject to the constraints of Eq. (6).

$$
\frac{1}{2} ||w||^2 + C \sum_{i=1}^{N} (\xi_i + \xi_i^*)
$$
\n(5)

$$
y_i - \mathbf{w}^{\mathrm{T}} \cdot \phi(\mathbf{x}_i) - b \le \varepsilon - \xi_i, \forall i = 1, \cdots, N
$$
 (6a)

$$
\mathbf{w}^{\mathrm{T}} \cdot \phi(\mathbf{x}_i) + b - y_i \le \varepsilon + \xi_i^*, \forall i = 1, \cdots, N
$$
 (6b)

$$
\xi_i \ge 0, \forall i = 1, \cdots, N \tag{6c}
$$

$$
\xi_i^* \ge 0, \forall i = 1, \cdots, N \tag{6d}
$$

208 where  $w$  is the coefficient factor,  $C$  is the box constraint,  $\varepsilon$  is the margin within which errors are 209 ignored,  $\xi_i$  and  $\xi_i^*$  are the slack variables,  $y_i$  is the response,  $x_i$  is the variable vector,  $\phi$  and *b* are 210 defined in the SVR approximation:

$$
f(x) = w^{\mathrm{T}} \cdot \phi(x) + b \tag{7}
$$

211 The slack variables,  $\xi_i$  and  $\xi_i^*$ , are introduced for each data point, and allow regression errors 212 to be larger than the margin error value,  $\varepsilon$ .

213 Eqs. (5) and (6) are transformed into the dual formula using the Lagrange multipliers <sup>28</sup>,  $\alpha_i$ 214 and  $\alpha_i^*$ .

$$
L(\alpha) = \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} (\alpha_i - \alpha_i^*) (\alpha_j - \alpha_j^*) K(x_i, x_j) + \varepsilon \sum_{i=1}^{N} (\alpha_i + \alpha_i^*) - \sum_{i=1}^{N} y_i (\alpha_i - \alpha_i^*)
$$
(8)

$$
\sum_{i=1}^{N} (\alpha_i - \alpha_i^*) = 0, \forall i = 1, \cdots, N
$$
\n(9a)

$$
0 \le \alpha_i \le C, \forall i = 1, \cdots, N \tag{9b}
$$

$$
0 \le \alpha_i^* \le C, \forall i = 1, \cdots, N \tag{9c}
$$

215 Instead of Eq. (5), Eq. (8) is minimized subject the constraints of Eq. (9).

216 In this work, the Gaussian kernel function  $29$  is used:

$$
K(x_i, x_j) \equiv \phi(x_i) \cdot \phi(x_j) = \exp\left(-\left\|x_i - x_j\right\|^2\right) \tag{10}
$$

217 Predictions of a response at given  $x$  is calculated according to,

$$
f(\mathbf{x}) = \sum_{i=1}^{N} (\alpha_i - \alpha_i^*) K(\mathbf{x}_i, \mathbf{x}) + b
$$
 (11)

218 The data are standardized before the model is trained. The SVR implementation in Matlab is 219 used. The training process of the SVR model is performed in nested loops:

- 220 In the outer loop, the SVR hyper parameters, i.e., the box constraint, kernel scale, and threshold,  $\varepsilon$ , are optimized using the Bayesian optimization  $30-32$  with the expected-222 improvement-plus algorithm  $30$  as the acquisition function to choose the next promising 223 hyper parameter set, which is expected to have smaller errors for the validation set.
- 224 In the inner loop, with fixed hyper parameters, the SVR model is optimized using the 225 sequential minimal optimization algorithm  $33$ .

226 In practice, the maximum number of iterations is set at 100, which turned out to be large enough 227 for convergence.

228 The SVR model is used in both the evaluation and correlation of the database. In the 229 evaluation, the entire database is used for training the SVR model in each step, as shown in Figure 230 1b.

 In the correlation, the obtained reference database is split into training, validation, and test sets. For each solution, 20% of the data are set aside as test sets; the remaining 80% of the data are used as training/validation sets. 10-fold cross-validation is implemented for training the SVR models. The accuracy of the model on the training/validation and test sets are investigated. An  executable program with user interface are provided in the Supplementary Material for calculations using the trained model.

#### <span id="page-12-0"></span>**2.5 Williams plot analysis**

238 In addition to the GMM analysis, the Williams plot analysis is employed for visualizing distribution of the selected data.

$$
h_i = \boldsymbol{x}_i \mathbf{X} (\boldsymbol{X}^{\mathrm{T}} \boldsymbol{X})^{-1} \boldsymbol{x}_i \tag{12}
$$

240 where  $h_i$  is the hat value,  $x_i$  is the variable vector of a data point, and *X* is the variable matrix of the entire database. The threshold value  $h^* = 3(P + 1)/N$  is also calculated and compared with 242 the hat value of all the data points, where  $P = 3$  is the number of variables, and *N* is the number of data points.

 In the Williams plot, the relative deviation of the SVR model is plotted against the hat value. 245 The approach is widely used for evaluating the applicability domain in QSAR models. When  $h_i$  >  $h^*$ , in QSAR models, the calculation is considered extrapolated and could be less reliable; however, for the density correlation here, the data point is considered to be located in a scarcer region. Because of the completeness of information in thermodynamic (3 degrees of freedom of the density of the mixture of water and a salt) as compared to the incompleteness of information for mapping between molecular structure and activity (as in QSAR models), the threshold can be considered much stricter here than in QSAR models. As will be discussed in Section 3 and in the Supplementary Material, deviations do not significantly increase beyond the threshold, indicating good correlation of the model in scarcer regions. Therefore, this threshold hat value of the database is not intended as a strict bar beyond which calculation should be prohibited. Instead, the threshold serves as merely an indicator that the calculations are made in scarcer regions.

 Furthermore, when calculations are made using the correlation, comparing the hat value of the calculations with the threshold and with the hat values of data points in the database visualizes whether the calculated data are located in a region where there are extensive data points that have been used in training the correlation.

#### <span id="page-13-0"></span>**3 Results and discussion**

 The collected datasets are evaluated using the procedure explained in Section 2. Table 2 provides the resulting reference database for the density of the 20 aqueous alkali halide solutions. 11081 data points of 586 datasets from 309 references are included in the database. The references are provided in the last column of the table. We recommend that these references be cited when using the database. The database is provided in the Supplementary Material. As an example, the (water + KCl) system is discussed in detail here. The plots for the other aqueous alkali halide solutions are provided in the Supplementary Material. Figure 3 shows the GMM plot for the density data of the (water + KCl) system. The contour is to visualize data distribution. The GMM is analyzed on the *T*-*x*ion projection, because most of the density data of the system are distributed at or near atmospheric pressure. The experimental data are plotted together with the contours.

271 Table 2. Reference database for the density of the 20 aqueous alkali halide solutions, and deviations of the SVR model. AAD is the percentage average absolute 272 deviation. MAD is the percentage maximum absolute deviation.

Water $+$	Collected data		Selected data								
	No. of data points	No. of datasets	No. of data points	No. of	T(K)	$x_{\rm ion}$	Reference	AAD(%)		MAD(%)	
				datasets				Training- Validation	Test	Training- Validation	Test
LiF	55	5	55	$\mathfrak{S}$	291.15-308.15	$0 - 0.0019$	$35 - 39$	0.0031	0.0014	0.12	0.0030
<b>NaF</b>	347	17	347	17	273.15-572.70	$0 - 0.019$	$36 - 52$	0.013	0.031	0.59	0.60
$\rm K \rm F$	465	18	448	14	293.15-572.70	$0 - 0.17$	36, 37, 42 - 47, 53 - 58	0.055	0.050	0.53	0.74
<b>RbF</b>	32	$\overline{4}$	32	$\overline{4}$	291.15-333.15	$0 - 0.067$	36, 42, 43, 59	0.057	0.084	0.42	0.37
CsF	27	3	27	3	293.15-333.15	$0 - 0.050$	36,42,43	0.15	0.13	0.42	0.27
LiCl	1650	77	1181	57	273.15-549.80	$0 - 0.27$	36,41-44,60-111	0.031	0.024	0.57	0.57
<b>NaCl</b>	3647	185	2687	137	253.00-573.35	$0 - 0.098$	41-44,48,54,93-223	0.018	0.012	0.25	0.16
<b>KCl</b>	2264	160	1624	105	273.15-473.15	$0 - 0.11$	40,41,43-45,53,54,91,92,99-111,196- 217,223-284	0.017	0.012	0.31	0.30
<b>RbCl</b>	301	30	168	14	288.15-328.15	$0 - 0.12$	41,43,44,52,54,101-104,123,223,281,282,285	0.064	0.10	0.34	0.36
<b>CsCl</b>	408	36	351	30	273.85-473.15	$0 - 0.19$	42, 43, 88, 91, 102 - 107, 119 - 124, 196, 217, 223, 282, 285-294	0.20	0.29	1.0	0.75
LiBr	939	25	698	19	229.15-525.00	$0 - 0.22$	36, 42, 43, 66-68, 97, 108, 109, 137, 285, 295-302	0.045	0.062	0.41	0.51
NaBr	1319	55	1204	37	273.15-549.80	$0 - 0.14$	36, 42 - 44, 62, 66, 73, 97, 108 - 110, 195, 217, 223 - 225, 282, 285 - 287, 302 - 317	0.055	0.040	1.0	0.39
KBr	1083	67	856	49	270.91-473.15	$0 - 0.12$	36,41-44,56,62,66,96,100,102,108,109,135- 138,213-217,221,224,229- 236, 282, 285, 290, 295, 302, 314, 315, 318 - 327	0.037	0.030	0.49	0.20
RbBr	77	6	38	$\overline{4}$	291.15-333.15	$0 - 0.074$	36, 42, 43, 52	0.082	0.048	0.41	0.070
CsBr	120	12	50	$\tau$	298.15-308.15	$0 - 0.073$	36, 43, 62, 88, 223, 286, 287	0.12	0.18	0.43	0.28
LiI	352	17	289	10	278.15-575.75	$0 - 0.12$	42,62,68,97,107,109,285,328-330	0.056	0.051	0.84	0.19
NaI	271	38	165	20	293.15-323.15	$0 - 0.15$	36, 43, 44, 54, 97, 102, 107- 109, 154, 237, 290, 298, 311, 331 - 336	0.095	0.085	1.7	0.15
KI	750	46	661	37	270.32-473.15	$0 - 0.13$	36,41,43-45,48,53,56,93,100,107- 109,154,212-216,235- 238, 282, 285, 290, 295, 305, 318, 322, 336-342	0.022	0.033	0.45	0.63
RbI	64	7	56	6	273.15-333.15	$0 - 0.11$	36, 42, 43, 52, 107, 137	0.21	0.28	0.87	0.38
CsI	144	11	144	11	273.15-343.34	$0 - 0.058$	35, 36, 42, 43, 107, 137, 223, 286, 287, 290, 343	0.093	0.13	0.46	0.38

273



 Figure 3. Gaussian mixture model for the density data of the (water + KCl) system. The contour plot is the calculated data-distribution-density. The dots are data points of the database.

 Based on the database, an SVR model is developed according to the procedure introduced in Section 2.4. Figure 4 shows the parity plot of the SVR correlation for the density of the (water + KCl) system. The test set is calculated with comparable accuracy compared to the training and validation sets. The SVR model is very accurate within the range of the database. Percentage average absolute deviation (AAD) and percentage maximum absolute deviation (MAD) for the 20 aqueous alkali halide solutions are provided in Table 2. The deviations are slightly larger compared to the maximum deviations in the data evaluation step, in which the models are trained on all the data of the aqueous alkali halide solutions (maximum deviations between the selected datasets do not exceed 1.1%, and are smaller than 0.5% for most of the aqueous alkali halide solutions). We expect that training the SVR model based on the entire database would slightly improve correlation accuracy without hampering the extrapolation performance of the model. However, we would not be able to verify this without any data for the test set. Therefore, 20% of the database is set aside as a test set.



291 Figure 4. Parity plot of the SVR correlation for the density of the (water  $+$  KCl) system.

 Figure 5 shows the Williams plot of the SVR correlation for the density data of the (water + KCl) system. There are some data points that exceed the threshold hat value. Most of these data points are at high pressure, while the majority in the database are at atmospheric pressure. However, deviations are not larger compared to the data points below the threshold. For the test set, the deviations are comparable to those of the training and validation sets. The good correlation and prediction show that the database is reliable on the edges of the data coverage, where there are much fewer data points, and that the SVR model is not over fitted. The Williams plot for the SVR model of the other aqueous alkali halide solutions are provided in the Supplementary Material. 300 The behavior is similar to that of the (water  $+$  KCl) system.



 Figure 5. Williams plot of the SVR correlation for the density data of the (water + KCl) system. The hat 303 values are calculated using Eq.  $(13)$  for the training & validation sets, and for the test set.

 An executable program is provided in the Supplementary Material for calculating density of the aqueous alkali halide solutions. Figure 6 shows an example of the user interface. Density results are provided along with data ranges of the solution, and illustrations of the calculations plotted on the Williams and GMM plots.



 Figure 6. Example of the user interface for density calculation. The salt is selected using the dropdown list on the top-left corner. Then, input can be made in the numeric edit fields, or imported from a file. A sample file is provided in the Supplementary Material. Then, at the click of the "Calculate" button, results are shown in the table on the right side. Notes about the calculation are displayed above the table, summarizing ranges of the database for the mixture, or, in the case of a calculation beyond the database ranges, warnings about which input variable exceeds the range. The Williams and GMM plots are shown on the bottom.

#### <span id="page-17-0"></span>**4 Conclusions**

 In this work, the experimental density data of 20 aqueous alkali halide solutions are extensively collected and critically evaluated using machine learning. A reference database

 consisting of 11081 data points of 586 datasets from 309 references is constructed. Maximum deviations between the selected datasets do not exceed 1.1%, and are smaller than 0.5% for most of the aqueous alkali halide solutions. Data distribution is visualized using the Williams plot and Gaussian mixture model. Support vector regression models are developed based on the database, and implemented in an executable program.

 The obtained database and models can be utilized in the development of electrolyte equations of state. The proposed data evaluation procedure for density can potentially be used for other properties that do not change drastically in the aqueous phase.

- <span id="page-18-0"></span>**5 Supplementary Material**
- The followings are provided in the Supplementary Material:
- An Excel file containing all the data.
- An executable program for density calculation.
- GMM and Williams plots for the aqueous alkali halide solutions.

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- <span id="page-18-2"></span>**6 Author Declarations**

# <span id="page-18-3"></span>**6.1 Conflict of Interest**

The authors declare no competing financial interest.

#### <span id="page-18-4"></span>**7 Data Availability Statement**

 The data that support the findings of this study are available within the article and its supplementary material.

## <span id="page-18-5"></span>**8 Reference**

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